Steady-state activation and modulation of the concatemeric α1β2γ2L GABA$_A$ receptor

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Abbreviations: 3α5αP, 5α-pregnan-3α-ol-20-one (allopregnanolone); c, ratio of the equilibrium

dissociation constant of the open receptor to that of the closed receptor; $GABA_A$ receptor, γ-

aminobutyric acid type A receptor; K, equilibrium dissociation constant of the closed receptor; L,

measure of unliganded activity calculated as ratio of resting to active receptors; P_{Active},

probability of being in the active state; $P_{Active,Peak}$, probability of being in the active state during

the peak response; $P_{Active,S.S.}$, probability of being in the active state during the steady-state

response; PS, pregnenolone sulfate; Q, measure of desensitization calculated as ratio of active

to desensitized receptors.

ABSTRACT

The two-state coagonist model has been successfully used to analyze and predict peak current responses of the $GABA_A$ receptor. The goal of the present study was to provide a model-based description of $GABA_A$ receptor activity under steady-state conditions after desensitization has occurred. We describe the derivation and properties of the cyclic three-state Resting-Active-Desensitized (RAD) model. Relationship of the model to receptor behavior was tested using concatemeric α1β2γ2 $GABA_A$ receptors expressed in *Xenopus* oocytes. The receptors were activated by the orthosteric agonists GABA or β-alanine, the allosteric agonist propofol, or combinations of GABA, propofol, pentobarbital and the steroid allopregnanolone, and the observed steady-state responses were compared with those predicted by the model. A modified RAD model was employed to analyze and describe the actions of the inhibitory steroid pregnenolone sulfate on steady-state current. The findings indicate that the steady-state activity in the presence of multiple active agents that interact with distinct binding sites follows standard energetic additivity. The derived equations enable prediction of peak and steady-state activity in the presence of orthosteric and allosteric agonists, and the inhibitory steroid pregnenolone sulfate.

Significance statement:

The study describes derivation and properties of a three-state Resting-Active-Desensitized model. The model and associated equations can be used to analyze and predict peak and steady-state activity in the presence of one or more active agents.

INTRODUCTION

The classic two-state concerted transition model (the MWC model) was originally introduced by Monod, Wyman and Changeux to study allosteric transitions in multimeric proteins (Monod et al., 1965). More recently, it has been employed to describe activation of transmitter-gated ion channels, including the GABA$_A$ receptor (Akk et al., 2018; Chang and Weiss, 1999; Ruesch et al., 2012). The model postulates two states for the receptor, resting and active. The receptor contains one or more functionally equivalent agonist binding sites, and receptor activation is driven by the higher affinity of the binding sites to the agonist in the active state. Only four parameters (extent of constitutive activity, affinity of the resting receptor to agonist, affinity of the active receptor to agonist, and the number of agonist binding sites) are required to describe receptor activation (Ehlert, 2014; Forman, 2012; Steinbach and Akk, 2019). Despite its simplicity, the MWC model has been shown to account for receptor activation by a number of orthosteric and allosteric agonists, and agonist combinations (Akk et al., 2018; Cao et al., 2018; Chang and Weiss, 1999; Ruesch et al., 2012; Ziemba and Forman, 2016).

Desensitization is explicitly excluded in the two-state model, which is therefore better suited to analyze peak, i.e., pseudo-steady-state, responses, and activity from receptors exhibiting weak desensitization such as the ρ subunit-containing GABA$_A$ receptor. However, for the majority of transmitter-gated ion channels, including the ubiquitous α1β2γ2 subtype of the GABA$_A$ receptor, desensitization is a fundamental property. Furthermore, for many endogenous and clinical GABAergic agents, steady-state, rather than peak, currents more appropriately reflect clinically relevant aspects of receptor function. To provide a tool to study, and predict, steady-state activity we expanded the two-state MWC model to include a desensitized state while retaining the concerted nature of state transitions. The three-state Resting-Active-Desensitized (abbreviated: RAD; Fig. 1A) model is a cyclic model with N identical sites for an agonist. The sites have low affinity to the agonist when the receptor is in the resting state, and

high affinity when the receptor is in the active or desensitized state. Like the classic MWC model, the three-state RAD model can be further expanded to describe steady-state activation in the presence of multiple agonists.

A modification of the model (Fig. 1B) was derived to describe the effect of the endogenous inhibitory steroid pregnenolone sulfate (PS). Coapplication of PS with GABA enhances apparent desensitization of the receptor (Akk et al., 2001; Eisenman et al., 2003). The modified RAD model contains N binding sites for pregnenolone sulfate that have high affinity in the desensitized state and low affinity in the active or resting states.

The relationship of the models to receptor behavior was tested using the concatemeric α1β2γ2 GABA$_A$ receptor expressed in *Xenopus* oocytes. The receptor was activated by several combinations of orthosteric (GABA, β-alanine) and allosteric (propofol, pentobarbital, 3α5αP, PS) agents. The observed data are compared to predictions made using the RAD model.

MATERIALS AND METHODS

Receptors and expression

The GABA$_A$ receptors were expressed in *Xenopus laevis* oocytes. Harvesting of oocytes was conducted under the Guide for the Care and Use of Laboratory Animals as adopted and promulgated by the National Institutes of Health. The animal protocol was approved by the Animal Studies Committee of Washington University in St. Louis (Approval No. 20170071).

The receptors consisted of concatemeric β2-α1-γ2L (βαγ) and β2-α1 (βα) constructs. The design and properties of the concatemeric receptors have been described previously (Bracamontes et al., 2011; Bracamontes and Steinbach, 2009). The cDNAs in the pcDNA3 vector were linearized with Xba I (NEB Labs, Ipswich, MA) and the cRNAs generated using mMessage mMachine (Ambion, Austin, TX). The oocytes were injected with a total of 10 ng cRNA in a 1:1 (βαγ:βα) ratio. Injected oocytes were incubated in bath solution (96 mM NaCl, 2 mM KCl, 1.8 mM CaCl$_2$, 1 mM MgCl$_2$, and 5 mM HEPES; pH 7.4) with supplements (2.5 mM Na pyruvate, 100 U/ml penicillin, 100 μg/ml streptomycin, and 50 μg/ml gentamycin) at 16^{0}C for 2-3 days prior to conducting electrophysiological recordings.

Electrophysiology

The recordings were conducted using standard two-electrode voltage clamp. The oocytes were clamped at -60 mV. The chamber (RC-1Z, Warner Instruments, Hamden, CT) was perfused with bath solution at 5-8 ml/min. Solutions were gravity-applied from 30-ml glass syringes with glass luer slips via Teflon tubing. Solutions were switched manually.

The current responses were amplified with an Axoclamp 900A (Molecular Devices, Sunnyvale, CA) or OC-725C amplifier (Warner Instruments, Hamden, CT), digitized with a Digidata 1320 or 1200 series digitizer (Molecular Devices), and stored using pClamp (Molecular

Devices).

A typical experiment entailed recording of a 10-20-s baseline, followed by a test agonist

application for 90-330 s (1.5-5.5 min), and bath application until full recovery. Due to long

exposure times, each cell was exposed to only 1 to 3 test concentrations of agonist rather than

a complete range of agonist concentrations. Thus, the concentration-response relationships

shown reflect average responses from cells exposed to an incomplete range of agonist

concentrations. The effects of the inhibitory steroid PS were determined by coapplying the

steroid with 1 mM or 3 µM GABA. Each cell was tested with 1-3 concentrations of PS. Each cell

was also tested with 3 mM GABA + 100 µM propofol to determine the maximal response to

which the responses to test drugs were compared.

Analysis of peak currents

The current traces were analyzed using Clampfit (Molecular Devices) to determine the peak

and steady-state amplitudes. In cases where the current response had not reached steady-state

(defined as ΔI <2% during the last 20 s of agonist application) by the end of the 4-5 min agonist

application, steady-state was estimated by exponential fitting of the current decay.

The current amplitudes were converted to units of probability of being in the active state

(P_{Active}), by matching the relative peak responses against a scale ranging from the P_{Active} of 0 to

1 (Eaton et al., 2016; Forman and Stewart, 2012). Wild-type concatemeric receptors in the

absence of agonist exhibit minuscule constitutive activity (P_{Active} = 0.00011) (Akk et al., 2018);

therefore, the holding current in the absence of agonists was considered to have a P_{Active}

indistinguishable from 0. The current level corresponding to P_{Active} of 1 was estimated by

exposing the receptors to the combination of 3 mM GABA and 100 µM propofol (Shin et al.,

2018). The values of P_{Active} in the presence of test agonists are expressed as mean ± S.D.

The activation parameters for peak currents were determined as described previously (e.g.,

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(Akk et al., 2018)). The peak currents, in P_{Active} units, were fitted with the following equation (Forman, 2012; Steinbach and Akk, 2019):

$$P_{Active,Peak,[X]} = \frac{1}{1 + L \times \left[\dfrac{1 + [X]/K_X}{1 + [X]/(K_X c_X)}\right]^{N_X}} \qquad (1)$$

where [X] is the concentration of agonist X, K_X is the equilibrium dissociation constant for agonist X in the resting receptor, c_X is the ratio of the equilibrium dissociation constant for X in the active receptor to K_X, and N_X is the number of binding sites for X. L expresses the level of background activity. L was constrained to 8000 (Akk et al., 2018). When the activity of X was studied in the presence of a low concentration of a background agonist Y, L was constrained to the value calculated as $(1-P_{Active,Y}) / P_{Active,Y}$. Curve-fitting was carried out using Origin v. 7.5 (OriginLab, Northhampton, MA) on pooled data from at least 5 cells. The fitted values for K_X and c_X are given as best-fit parameter ± standard error of the fit.

Predictions for current responses

The predictions for peak current responses were made as described in detail previously (Shin et al., 2019). In brief, the P_{Active} was calculated using the state function (Eq. 1) that pertains to the two-state MWC model (Forman, 2012; Steinbach and Akk, 2019). The activation parameters (receptor affinity and efficacy) were taken from earlier studies (Akk et al., 2018; Shin et al., 2018; Shin et al., 2017). The predictions for the probability of being in the active state during the steady-state response ($P_{Active,S.S.}$) were made using Eqs. 4 (for a single agonist) or 25 (for agonist combinations) that pertain to the three-state model that incorporates a desensitized state (Fig. 1). More details are provided below.

When predicting responses to two or more agonists the nominal concentration of each agonist was adjusted to account for cell-to-cell variability (Shin et al., 2019). By matching the

relative experimental peak response to the previously determined concentration-response relationship, the predicted response to a combination of agonists is based on the observed P_{Active} of responses to individual agonists rather than the nominal concentrations of the individual agonists. For example, the predicted response to GABA + propofol is calculated based on the observed responses to GABA and propofol applied separately, rather than on the nominal concentrations of GABA and propofol.

Materials and chemicals

The inorganic salts used to prepare the bath solution and GABA were purchased from Sigma-Aldrich (St. Louis, MO). Propofol was purchased from MP Biomedicals (Solon, OH). The steroids 3α5αP and pregnenolone sulfate (PS) were bought from Sigma-Aldrich or Tocris (Bio-Techne, Minneapolis, MN).

The stock solution of GABA was made in the bath solution at 500 mM, stored in aliquots at -20°C, and diluted on the day of experiment. The solution of β-alanine was made in 30 mM in bath solution on the day of experiment. Stock solution of propofol was made in DMSO at 200 mM and stored at room temperature. 3α5αP was dissolved in DMSO at 10-20 mM and stored at room temperature. PS was dissolved in DMSO at 50 mM and stored at 4^{0}C.

RESULTS

Description of the three-state model

The two-state MWC model (Forman, 2012; Steinbach and Akk, 2019) can be readily

extended to include a desensitized state originating from the active state. We have termed the

modified, three-state model as the Resting-Active-Desensitized (or the "RAD") model (Fig. 1).

The model retains the concerted nature of the state transitions, i.e., all sites undergo identical

and simultaneous state transition. In the absence of agonist, L=R/A and Q=A/D. The ratio of the

dissociation constant for the high-affinity state to that for the low-affinity state is c_X; the affinity of

the desensitized state to the agonist is postulated to be identical to that of the active state, as

has been shown experimentally for the related nicotinic receptor (Edelstein et al., 1996;

Grosman and Auerbach, 2001; Sine et al., 1995).

The equilibrium probability of being high-affinity, i.e., in an active or desensitized state is

described by the following equation:

$$P_{High} = \frac{1}{1+\left[\dfrac{LQ}{1+Q}\right]\left[\dfrac{(1+[X]/K_X)}{(1+[X]/c_X K_X)}\right]^{N_x}} = \frac{1}{1+\left[\dfrac{LQ}{1+Q}\right]\Gamma_{[X]}} \qquad (2)$$

where we define

$$\Gamma_{[X]} = \left[\frac{1+[X]/K_X}{1+[X]/(c_X K_X)}\right]^{N_X} \qquad (3)$$

The probability of being active is the probability of being active given that the receptor is

high-affinity times the probability the receptor is high-affinity, where Prob[Active given Active or

Desensitized] = Q/(1 + Q).

$$P_{Active,[X]} = \frac{Q/(1+Q)}{1+\left[\dfrac{LQ}{1+Q}\right]\Gamma_{[X]}} = \frac{1}{1+\dfrac{1}{Q}+L\Gamma_{[X]}} \qquad (4)$$

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Eq. 4 can be used to estimate activity under steady-state conditions. As Q→∞ (or 1/Q = D/A→0, i.e., minimal desensitization), P_{Active} approaches

$$P_{Active,[X]}{}^{*} = \frac{1}{1+L\Gamma_{[X]}}$$

(5)

As [X] → 0 (no agonist), P_{Active} approaches

$$P_{Active,[X]=0} = \frac{1}{1+\dfrac{1}{Q}+L}$$

(6)

and as [X] → ∞ (saturating agonist), P_{Active} approaches

$$P_{Active,[X]=\infty} = \frac{1}{1+\dfrac{1}{Q}+Lc_X{}^{N_X}}$$

(7)

The equation for the normalized EC_{50} for activation is similar to that for the two-state MWC model. To emphasize the similarity, let μ=1+1/Q:

$$\gamma_X = \frac{EC_{50}}{c_X K_X} = \frac{\{\mu + \mu c_X{}^{N_X} + 2Lc_X{}^{N_X}\}^{1/N_X} - \{2\mu + Lc_X{}^{N_X} + L\}^{1/N_X}}{c_X\{2\mu + Lc_X{}^{N_X} + L\}^{1/N_X} - \{\mu + \mu c_X{}^{N_X} + 2Lc_X{}^{N_X}\}^{1/N_X}}$$

(8)

As L → 0 (low energy of activation)

$$\gamma_X \to \frac{(\mu(1+c_X{}^{N_X}))^{1/N_X} - 2\mu^{1/N_X}}{c_X{}^{N_X} 2^{1/N_X} - (\mu(1+c_X{}^{N_X}))^{1/N_X}}$$

(9)

As L → ∞ (high energy of activation)

$$\gamma_X \to \frac{(2c_X{}^{N_X})^{1/N_X} - (1+c_X{}^{N_X})^{1/N_X}}{c_X(1+c_X{}^{N_X})^{1/N_X} - c_X}$$

(10)

As Q → 0 (strong desensitization)

(11)

$$\gamma_X \to \frac{(1+c_X{}^{N_X})^{1/N_X} - 2^{1/N_X}}{c_X 2^{1/N_X} - (1+c_X{}^{N_X})^{1/N_X}}$$

As $Q \to \infty$ (weak desensitization), Υ_X approaches the value for the two-state MWC model with those values of L and c_X.

$$\gamma_X \to \frac{(1 + c_X{}^{N_X} + 2Lc_X{}^{N_X})^{1/N_X} - (2 + L + Lc_X{}^{N_X})^{1/N_X}}{c_X(2 + L + Lc_X{}^{N_X})^{1/N_X} - (1 + c_X{}^{N_X} + 2Lc_X{}^{N_X})^{1/N_X}}$$

(12)

The probability of being desensitized is

$$P_{D,[X]} = \frac{1/(1+Q)}{1 + LQ/(1+Q)\Gamma_{[X]}} = \frac{1}{1 + Q + LQ\Gamma_{[X]}}$$

(13)

In the absence of agonist

$$P_{D,[X]=0} = \frac{1}{1 + Q + QL} = \frac{1}{1 + Q(1+L)}$$

(14)

And at saturating agonist

$$P_{D,[X]=\infty} = \frac{1}{1 + Q + QLc_X{}^{N_X}} = \frac{1}{1 + Q(1 + Lc_x{}^{N_X})}$$

(15)

The relative probability of being active at steady-state, i.e., the ratio of the probabilities of being in the active state at steady-state vs. peak is:

$$\Psi_{[X]} = \frac{P_{Active,[X]}}{P_{Active,[X]}{}^*} = \frac{1/(1 + \frac{1}{Q} + L\Gamma_{[X]})}{1/(1 + L\Gamma_{[X]})} = \frac{1 + L\Gamma_{[X]}}{1 + \frac{1}{Q} + L\Gamma_{[X]}}$$

(16)

When Q is large (minimal desensitization), then Ψ_X approaches 1. The constitutive relative probability of being open in the absence of agonist is

$$\Psi_{[X]=0} = \frac{1 + L}{1 + \frac{1}{Q} + L}$$

(17)

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The relative probability of being active in the presence of a saturating concentration of X is:

$$\Psi_{[X]=\infty} = \frac{1 + Lc_X^{N_X}}{1 + \dfrac{1}{Q} + Lc_X^{N_X}} \qquad (18)$$

When $c_X = 1$ (competitive antagonist) then $\Psi_{[X]=0} = \Psi_{[X]=\infty}$, while when $c_X < 1$ (agonist) then

$\Psi_{[X]=0} > \Psi_{[X]=\infty}$.

An illustration of receptor behavior

Figure 2 illustrates a simulated current response and its relation to the kinetic scheme. On the left, a graph is shown of the states of the receptor (resting, active and desensitized) with the fractions of the population indicated by the lines. A cartoon of a response to an application of agonist X is shown on the right. The parameters discussed are indicated on the cartoon.

Two important assumptions are made in the analysis of the peak response. First, the peak response is not affected by development of desensitization (i.e., desensitization is slow). The second assumption is that the maximal potentiated response activates all receptors that were not desensitized in the steady-state before the application of agonist. This assumption is also made for the analysis of responses in terms of the two-state MWC model, and allows the response to be converted to the probability of being active.

The total range of response is:

$$Z_{max} = I_{Max} - I_{PTX} = (\text{scale}) \times 1 \times (1 - D_0) \qquad (19)$$

where "scale" converts probability of being active to current. The maximal probability of being active ($P_{Active,max}$) is assumed to be 1, and D_0 is the probability a receptor is desensitized in the absence of agonist.

The normalized peak response to a given concentration of agonist X is then given as:

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$$P_{Active,Peak,[X]} = \frac{Z_{Peak,[X]}}{Z_{Max}} = \frac{I_{Peak,[X]} - I_{PTX}}{I_{max} - I_{PTX}} = \frac{(scale) \times P_{Active,Peak,[X]} \times (1-D_0)}{(scale) \times (1-D_0)}$$

(20)

Under the assumption that the peak response is not affected by the development of desensitization, then the normalized peak response can be analyzed in terms of the two-state MWC model to yield estimates of K_X and c_X. The steady-state response can be analyzed in terms of the relative response compared to the peak. An earlier result gave an equation for the relative probability of being active. We can define the relative probability of being active from the steady-state (fully desensitized) response to [X] relative to the peak response to [X]:

$$\Psi_{[X]} = \frac{Z_{S.S.,[X]} / Z_{Max}}{Z_{Peak,[X]} / Z_{Max}} = \frac{P_{Active,S.S.,[X]}}{P_{Active,Peak,[X]}^*} = \frac{1/(1 + \frac{1}{Q} + L\Gamma_{[X]})}{1/(1 + L\Gamma_{[X]})} = \frac{1 + L\Gamma_{[X]}}{1 + \frac{1}{Q} + L\Gamma_{[X]}}$$

(21)

There are estimates for all the terms in the equation except for Q, so Q can be estimated from the concentration dependence of $\Psi_{[X]}$.

Peak and steady-state activation of the concatemeric α1β2γ2L GABA_A receptor by GABA

Cells expressing concatemeric α1β2γ2L receptors were exposed to 90-330 s applications of 0.3-1000 µM GABA. To minimize various errors associated with long-duration recordings, each cell was exposed to only 1-3 test concentrations of GABA rather than to a full range of agonist concentrations. Each cell was also tested with 3 mM GABA + 100 µM propofol that was considered to activate all receptors that were not desensitized prior to drug application (Shin et al., 2018). Sample current responses and the concentration-response data for peak and steady-state currents are shown in Fig. 3.

Channel activity was analyzed by first determining the activation parameters (K_{GABA}, c_{GABA}) from peak currents using Eq. 1. In the second step, the steady-state currents from the same set of cells were analyzed using Eq. 4, with K_{GABA} and c_{GABA} constrained to the values determined in the analysis of peak responses.

From the analysis of peak responses, we estimate a K_{GABA} of 59 ± 22 μM (best-fit parameter ± S.E. of the fit) and a c_{GABA} of 0.0020 ± 0.0006. The number of binding sites for GABA was constrained to 2, and L was held at 8000 (Akk et al., 2018). The estimated values for K_{GABA} and c_{GABA} are similar to our previous estimates (K_{GABA} = 72 μM, c_{GABA} = 0.0033), obtained from experiments in which each cell was exposed to short-duration applications of the full range of agonist concentrations (Akk et al., 2018).

To determine the value of Q (=A/D in the RAD model; Fig. 1), we fitted the concentration-response curve for steady-state currents using Eq. 4. The values of K_{GABA} and c_{GABA} were constrained to those obtained from fitting the peak currents in the same set of cells (59 μM and 0.0020, respectively). Curve-fitting the concentration-response data yielded a Q of 0.27 ± 0.02. Thus, under steady-state conditions, the ratio of active to desensitized receptors is ~1:4 for the α1β2γ2L concatemeric receptor.

Peak and steady-state activation of the concatemeric α1β2γ2L GABA$_A$ receptor by propofol

We next determined receptor desensitization properties in the presence of the allosteric agonist propofol. In the RAD model, desensitization, determined by the parameter Q, is a property of the receptor rather than agonist. Accordingly, we expected that the values of Q are similar in the presence of propofol and GABA.

To shift the propofol concentration-response relationship to lower concentrations and to reduce propofol-induced block (Ruesch et al., 2012; Shin et al., 2018), the recordings were

conducted in the presence of a low concentration (3 µM) of GABA. The probability of being in

the active state in the presence of 3 µM GABA alone was 0.033 ± 0.026 (mean ± S.D.; n = 47

cells). Propofol concentration-response relationships were obtained by exposing each cell to 3

µM GABA alone, followed by GABA combined with 1-3 concentrations of propofol. Additionally,

each cell was tested with 3 mM GABA + 100 µM propofol. Sample currents and the

concentration-response relationships for peak and steady-state currents are shown in Fig. 4.

Analysis of the peak responses yielded a K_{PRO} of 10 ± 2 µM and a c_{PRO} of 0.37 ± 0.02. The

number of propofol binding sites, N_{PRO} was constrained to 6 (Shin et al., 2018), and the value of

L, calculated from the background activity as $(1-P_{Active,3 µM GABA})/ P_{Active,3 µM GABA}$, was constrained

to 29. The fitted K_{PRO} and c_{PRO} values are similar to previously reported values for the

concatemeric receptor (K_{PRO} = 21 µM and c_{PRO} = 0.22; (Shin et al., 2018)). Analysis of the

steady-state responses using Eq. 4, and the K_{PRO} and c_{PRO} constrained to the values obtained in

fitting the peak responses, yielded a Q of 0.36 ± 0.04.

Desensitization in the presence of a saturating concentration of strong agonist

In the RAD model, activation and desensitization are fully coupled at steady-state, so

agonists activate and desensitize with relative desensitization determined solely by Q (=A/D;

Fig. 1). If drug X is an efficacious agonist (c_X<<1) then at saturating concentrations of X the term

$L\Gamma_X$ in Eq. 22 will become very small and the probability of being active approaches Q/(1+Q):

$$P_{Active,[X]=\infty} = \frac{1}{1+\dfrac{1}{Q}+L\Gamma_{[X]}} \rightarrow \frac{Q}{1+Q} \qquad (22)$$

This will be true for all high-efficacy agonists, so relative desensitization is predicted to be

constant in the presence of all high-efficacy agonists and agonist combinations.

We tested this prediction by comparing $P_{Active,S.S.}$ in the presence of two efficacious orthosteric

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agonists, GABA and β-alanine. The agonists were applied at saturating concentrations: 1 mM

for GABA and 30 mM for β-alanine. Using the previously reported activation parameters for

GABA and β-alanine (Shin et al., 2019), the estimated $L\Gamma_{GABA}$ is 0.10 and $L\Gamma_{\beta\text{-alanine}}$ 0.05. The

steady-state probability of being active was determined by comparing the steady-state current

level to the peak amplitude, while taking into consideration the estimated P_{Active} of the peak

response at saturating agonist concentration (0.92 for GABA and 0.96 for β-alanine; (Shin et al.,

2019)). In the presence of 1 mM GABA, the $P_{Active,S.S.}$ was 0.16 ± 0.04 (mean ± S.D.; n = 9), and

in the presence of 30 mM β-alanine, the $P_{Active,S.S.}$ was 0.19 ± 0.06 (n = 7). Sample current

traces and data summary are given in Fig. 5. The calculated values for Q are 0.19 ± 0.06 for

GABA and 0.24 ± 0.08 for β-alanine.

Coapplication of an allosteric agonist with saturating GABA did not affect desensitization (Fig.

5). The $P_{Active,S.S.}$ was 0.22 ± 0.03 (n = 5), 0.19 ± 0.05 (n = 8), and 0.17 ± 0.11 (n = 6) in cells

exposed to 1 mM GABA combined with 20 μM propofol, 50 μM pentobarbital, or 1 μM 3α5αP,

respectively. The calculated Q values are 0.29 ± 0.04 for GABA + propofol, 0.24 ± 0.08 for

GABA + pentobarbital, and 0.23 ± 0.20 for GABA + 3α5αP. We propose that propofol,

pentobarbital, and allopregnanolone have minimal effect on the value of Q, i.e., the ratio of

active to desensitized receptors.

Effect of pregnenolone sulfate on steady-state current

The steroid pregnenolone sulfate (PS) inhibits the GABA$_A$ receptor. Previous work using

single-channel patch clamp has indicated that PS acts by reducing the mean duration of the

single-channel cluster without affecting intracluster open and closed time distributions (Akk et

al., 2001). In whole-cell recordings, the effect manifests as more rapid apparent desensitization

with minimal effect on peak amplitude (Eisenman et al., 2003). The data indicate that PS acts by

altering apparent desensitization.

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We examined the effect of 0.01-50 μM PS on steady-state current in the concatemeric

α1β2γ2L receptor activated by a saturating concentration (1 mM) of GABA. To minimize error

associated with multiple long-duration drug applications on the same cell, each cell was

exposed to 1-3 concentrations of PS rather than to the complete range of steroid

concentrations. Thus, the concentration-response relationships indicate pooled data of average

responses from cells exposed to an incomplete range of concentrations. Curve fitting the PS

concentration-response relationship with the Hill equation yielded an IC_{50} of 0.24 ± 0.03 μM

(best-fit parameter ± standard error of the fit). A sample current response is shown in Fig. 6A.

Further analysis was conducted in the framework of the modified RAD model (Fig. 1B). In this

model, PS binds with high affinity to the desensitized state resulting in receptor accumulation in

the desensitized state and inhibition of current response. The model does not require

modification of receptor properties (L or Q) or parameters of activation by agonist X (K_X or c_X).

For receptors activated by agonist X, the probability of being in the active state in the presence

of PS is:

$$P_{\text{Active},[X]} = \cfrac{1}{1+\cfrac{1}{Q}\times\left(\cfrac{1+[PS]/(c_{PS}K_{PS})}{1+[PS]/K_{PS}}\right)+L\Gamma_{[X]}} \tag{23}$$

where [PS] is the concentration of the steroid, K_{PS} is the equilibrium dissociation constant of the

resting and active receptor to PS, c_{PS} is the ratio of the equilibrium dissociation constant of the

desensitized receptor to K_{PS}. The number of sites for PS is assumed to be 1. For PS to shift

equilibrium towards the desensitized state, i.e., reduce receptor activity, $c_{PS} < 1$. $\Gamma_{[X]}$ is described

by Eq. 3. Fitting the PS concentration-response data to Eq. 23 yielded a Q of 0.31 ± 0.01, K_{PS} of

3.5 ± 1.2 μM, and c_{PS} of 0.054 ± 0.014. $L\Gamma_{GABA}$ was held at 0.10. The fitted value for Q is close to

that estimated for responses to GABA. The fitted curve is shown in Fig. 6B. We note that

inhibition at high concentrations of PS does not seem to be complete (Fig. 6B, inset), in

agreement with predictions made by Eq. 23.

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The position of the concentration-response relationship for PS-mediated inhibition of steady-state activity depends on the concentration of GABA used to activate the receptor. For this kinetic mechanism, the potency of PS would decrease when the fraction of receptors that is active decreases since a smaller fraction of receptors would be available to interact with high affinity. For receptors activated by 3 µM GABA ($<EC_5$), the IC_{50} was 4.0 ± 1.1 µM (best fit parameter ± standard error of the fit). A sample current trace is shown in Fig. 6C. To test whether the model can account for the increase in IC_{50} at a lower concentration of GABA, we simulated the concentration-response relationship for PS-mediated inhibition in the presence of 3 µM GABA using Eq. 23. The predicted curve and the observed data are shown in Fig. 6D. It is important to note that the predicted curve was generated with no free parameters. The term $L\Gamma_{GABA}$ was calculated from the observed response in the absence of PS, and other parameters were estimated from the fit to data with 1 mM GABA.

Effects of agonist combinations on steady-state currents

As in the case of the classic two-state MWC model, coapplication of agonist Y affects the action of agonist X by a change in the effective value of L when the two drugs interact with distinct sites. The probability of being in the high-affinity state is:

$$P_{High} = \frac{1}{1 + \left[\dfrac{LQ}{1+Q}\right]\Gamma_{[X]}\Gamma_{[Y]}} \tag{24}$$

and the probability of being in the active state is:

$$P_{Active,[X],[Y]} = \frac{Q/(1+Q)}{1 + \left[\dfrac{LQ}{1+Q}\right]\Gamma_{[X]}\Gamma_{[Y]}} = \frac{1}{1 + \dfrac{1}{Q} + L\Gamma_{[X]}\Gamma_{[Y]}} \tag{25}$$

The denominator in Eq. 25 can be modified with additional Γ terms for additional agonists.

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To confirm the prediction experimentally, we measured peak and steady-state activity in the presence of a triple agonist combination of 2 μM GABA + 0.15 μM 3α5αP + 5 μM propofol. In 6 cells, the mean $P_{Active,Peak}$ was 0.59 ± 0.13 and the mean $P_{Active,S.S.}$ 0.23 ± 0.03. The $P_{Active,S.S.}$ calculated using Eq. 4 with the value of Q constrained to 0.3, is 0.20 ± 0.01. Fig. 7A shows a comparison of predicted vs. observed $P_{Active,S.S.}/P_{Active,Peak}$ as a function of $P_{Active,Peak}$ for several additional combinations of orthosteric and allosteric agonists.

We further tested the independence of drug actions by determining the inhibitory effect of PS on receptors activated by various combinations of agonists. Fig. 7B shows the comparison of observed data with predictions made assuming independence of the actions of PS and various agonists. The predictions for steady-state open probability in the presence of PS and combinations of agonists were made using the following equation:

$$P_{Active,[X],[Y],[Z]} = \cfrac{1}{1 + \cfrac{1}{Q} \times \left(\cfrac{1 + [PS]/(c_{PS}K_{PS})}{1 + [PS]/K_{PS}} \right) + L\Gamma_{[X]}\Gamma_{[Y]}\Gamma_{[Z]}}$$

(26)

where X, Y, and Z denote the individual agonists (e.g., GABA, 3α5αP and propofol), and the term Γ is described by Eq. 3. The underlying assumptions in Eq. 26, that GABA, propofol, 3α5αP and PS interact with distinct binding sites, are supported by previous observations (Akk et al., 2001; Park-Chung et al., 1999; Ruesch et al., 2012; Shin et al., 2019).

The data indicate that for combinations of GABA + 3α5αP, GABA + propofol, and GABA + 3α5αP + propofol, there is good agreement between the predicted effect of PS and the observed data (Fig. 7B). Overall, the findings demonstrate independence of the actions of GABA, 3α5αP, propofol, and PS in generating steady-state activity.

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DISCUSSION

The major goal of this study was to develop a model to analyze steady-state activity in the

GABA$_A$ receptor. Most subtypes of the GABA$_A$ receptor, including the synaptic α1β2γ2 isoform,

exhibit marked desensitization during prolonged application of agonist. While synaptic receptors

are most prominently activated phasically during transient increase in GABA in the synaptic cleft

many other GABAergic agents are present chronically in the brain. These include taurine,

endogenous neuroactive steroids, and, under clinical conditions, various GABAergic anxiolytic

and sedative agents. Furthermore, tonic activation of extrasynaptic receptors by ambient GABA

is best described through steady-state activity.

We present and describe the properties of a three-state Resting-Active-Desensitized (RAD)

model (Fig. 1). The model retains salient features of the classic two-state Resting-Active MWC

model, including the concerted nature of state transitions (Ehlert, 2014; Forman, 2012;

Steinbach and Akk, 2019). In the two-state model, full description of channel activation is

described by 4 parameters: the extent of unliganded gating that is an inherent property of the

receptor, affinity of the resting receptor to agonist, affinity of the active receptor to agonist, and

the number of binding sites for the agonist. The additional transition to the desensitized state in

the RAD model is defined by a parameter (termed Q in the present study) describing equilibrium

between the active and desensitized states. The value of Q can be determined by fitting the

concentration-response curve for steady-state activity to Eq. 4. Alternatively, for high-efficacy

agonists or agonist combinations, Q can be estimated directly from a single high-concentration

response using Eq. 22.

The fitted value of Q was 0.27 in the concatemeric α1β2γ2L receptor activated by GABA. The

value of Q was similar in receptors activated by a saturating concentration of β-alanine (0.24) or

when a saturating concentration of GABA was coapplied with propofol (0.29), pentobarbital

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(0.24) or 3α5αP (0.23). In other words, under conditions where most receptors are active during the peak response, ~4 out of 5 receptors become desensitized once steady-state is reached.

The RAD model contains a single desensitized state. Previous study of the γ-containing GABA$_A$ receptor has indicated multiple desensitized/non-conducting states, with desensitization time constants associated with these states ranging from 3 ms to 10 s (Barberis et al., 2007; Bianchi and Macdonald, 2002; Feng et al., 2004). It is unlikely that the reduction of desensitization to a single high-affinity non-conducting state fundamentally affects the value of Q, which is associated with steady-state open probability and thus not directly dependent on the number of desensitized states.

Previous work has indicated that many GABA$_A$ receptor agonists act independently and energetically additively in producing peak currents (Cao et al., 2018; Ruesch et al., 2012; Rusch et al., 2004; Shin et al., 2019). This means that the actions of each drug in a combination can be considered separately with no necessity to invoke specific interactions between the combined drugs. Independence and additivity also readily enable prediction of peak amplitudes for any combination of agonists. The present study suggests that independence and energetic additivity similarly apply to steady-state currents in the presence of combinations of GABA, the steroid 3α5αP, and propofol.

The steroid PS inhibits the response of the GABA$_A$ receptor to GABA, and previous work has suggested that it acts by enhancing the probability that the receptor will be desensitized (Akk et al., 2001; Eisenman et al., 2003). The ability of PS to inhibit can be quantitatively described by the RAD model, assuming that PS binds preferentially to the desensitized state. It is clear that several other possible mechanisms cannot describe this inhibition. For example, it could be that PS binds to a site other than GABA and reduces receptor function by selectively binding to the resting state (Steinbach and Akk, 2019). In this case, PS would be more potent at lower concentrations of GABA, while we observe the opposite. An alternative is that PS is an open-channel blocker (i.e., it binds to and inhibits receptors in the A state), although single-channel

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data do not support this model (Akk et al., 2001). Also, in this case, the potency would decrease when a lower concentration of GABA is used to activate, but the inhibition would be complete at high concentrations of PS, unlike what is observed and shown in Fig. 6.

The RAD model (Fig. 1) can describe the steady-state activity in the presence of combinations of orthosteric and allosteric GABAergic agonists that interact with distinct sites. Furthermore, an extension of the model, expressed through Eq. 26, can be used to predict steady-state open probability in the presence of any combination of GABA, 3α5αP, propofol, and PS.

The original MWC and the RAD models have the fundamental aspect that multiple compounds interact to increase or reduce receptor activity by independently making energetic contributions to the stabilization of particular states (resting, active or desensitized). That is, drugs do not alter basic properties of the receptor (L or Q) nor activation properties of other agents (K_X, c_X or N_X). Energetic additivity is supported in the wild-type $GABA_A$ receptor by studies of agonist combinations (Akk et al., 2018; Cao et al., 2018; Ruesch et al., 2012; Rusch et al., 2004; Shin et al., 2017), and has been observed in some studies comparing the effects of mutations to individual binding sites for anesthetics (Guitchounts et al., 2012; Shin et al., 2018). In contrast, energetic additivity was found notably missing in a recent study that demonstrated that mutations to residues abutting and nonabutting the anesthetic binding sites could reduce anesthetic sensitivity (Szabo et al., 2019). Finally, lack of energetic additivity, and a potential for allosteric interaction between individual sites, have been shown for the two functional binding sites for steroids located in the α subunit and at the β-α interface (Chen et al., 2019). It is perhaps not surprising that structural changes can have allosteric effects in a receptor that clearly has a conformationally plastic structure. In sum, simple schemes based on the concerted transition model can be remarkably successful in quantitative predictions based on the idea that mutations or drug-binding events make independent and additive contributions to the energies of particular states.

AUTHORSHIP CONTRIBUTIONS

Participated in research design: Steinbach, Akk

Conducted experiments: Germann, Pierce, Burbridge

Contributed new reagents or analytical tools: N/A

Performed data analysis: Germann, Pierce, Burbridge, Akk

Wrote or contributed to the writing of the manuscript: Germann, Pierce, Burbridge, Steinbach, Akk

Footnotes

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Legends for Figures

Figure 1. The Resting-Active-Desensitized (RAD) model. Panel **A** gives the kinetic scheme for the standard RAD model, shown with two binding sites for agonist X. The receptor can occupy a resting (R), active (A), or desensitized (D) state. The active and desensitized states have high affinity to X while the resting state has low affinity to X. The parameter L (=R/A) describes the equilibrium between the resting and active states, and the parameter Q (=A/D) describes the equilibrium between the active and desensitized states. The parameter K_X is the equilibrium dissociation constant for X in the resting receptor. The parameter $c_X K_X$ is the equilibrium dissociation constant for X in the active and desensitized receptors. The classic MWC model contains only R and A states with no other modifications in states or equilibrium constants. Panel **B** shows a modification of the RAD model where the drug X has low affinity to resting and active states, and high affinity to the desensitized state. The modified model was employed to analyze receptor behavior in the presence of the inhibitory steroid pregnenolone sulfate.

Figure 2. Illustration of receptor behavior. The left panel shows the states of the receptor (resting, active and desensitized). The fractions of the populations in each state are shown by the arrows (dotted, resting receptor; solid, active receptor; dashed, desensitized receptor). D_0 is the fraction of desensitized receptors in the absence of agonist. The right panel shows a simulated current response to application of agonist X over the time indicated by the striped bar above the trace. I_{PTX} shows the level of constitutive activity as determined by blocking the constitutively active receptors with picrotoxin. $I_{Peak,[X]}$ gives the peak response to X, I_{Max} shows the peak response to agonist or combination of agonists eliciting a response with P_{Open} of 1. $I_{S.S.,[X]}$ is the steady-state current level in the presence of X. $Z_{Peak,[X]}$ is the total current at the peak of the response and equals to $I_{Peak,[X]}$ - I_{PTX}.

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Figure 3. Peak and steady-state activation by GABA. Panel **A** shows sample current traces from cells expressing wild-type concatemeric α1β2γ2L receptors activated by 1, 10, 100, or 1000 μM GABA. The dashed lines show the steady-state current levels as determined by exponential fitting of the decay phase. Panel **B** shows the concentration-response relationships for peak and steady-state currents. The data points show mean ± S.D. from 5-6 cells per concentration. The curves were fitted with Eqs. 1 and 4, respectively. The best-fit parameters for peak currents are: K_{GABA} = 59 ± 22 μM and c_{GABA} = 0.0020 ± 0.0006. The curve for steady-state currents was fitted using the K_{GABA} and c_{GABA} values constrained to those obtained in fitting the peak currents. The best-fit value for Q was 0.27 ± 0.02. The value of L was constrained to 8000 (Akk et al., 2018), and the number of binding sites for GABA was constrained to 2.

Figure 4. Peak and steady-state activation by propofol. Panel **A** shows sample current traces from cells expressing wild-type concatemeric α1β2γ2L receptors activated by 3 μM GABA (grey traces and grey time scales) and 3 μM GABA combined with 0.1, 0.5, 5, or 20 μM propofol (PRO; black traces and black time scales). The dashed lines show the steady-state current levels for GABA + propofol, as determined by exponential fitting of the decay phase. Panel **B** shows the concentration-response relationships for peak and steady-state currents. The data points show mean ± S.D. from 5-6 cells per concentration. The curves were fitted with Eqs. 1 and 4, respectively. The best-fit parameters for peak currents are: K_{PRO} = 10 ± 2 μM and c_{PRO} = 0.37 ± 0.02. The curve for steady-state currents was fitted using the K_{PRO} and c_{PRO} values constrained to those obtained in fitting the peak currents. The best-fit value for Q was 0.36 ± 0.04. The value of L was constrained to 29 as determined from background open probability in the presence of 3 μM GABA. The number of binding sites for propofol was constrained to 6 (Shin et al., 2018).

Figure 5. Comparison of desensitization to maximal responses to orthosteric agonists or combinations of orthosteric and allosteric agonists. Panel **A** shows sample traces in the presence of 30 mM β-alanine, and 1 mM GABA combined with 20 μM propofol, 50 μM pentobarbital or 1 μM 3α5αP. The dashed lines show the level of steady-state current, estimated by exponential fitting of the decay phase. A representative trace for 1 mM GABA is provided in Fig. 3A. Panel **B** gives the steady-state open probability in the presence of GABA, β-alanine, or combinations of GABA and an allosteric agonist. The open symbols show responses from individual cells (5-9 cells per condition). The filled symbols and error bars give mean ± S.D. while the horizontal lines show the grand mean (solid line) ± S.D. (dashed lines) for the entire data set.

Figure 6. Receptor inhibition by the steroid pregnenolone sulfate. Panel **A** gives a sample current trace showing the effect of 10 μM pregnenolone sulfate (PS) on concatemeric α1β2γ2L receptors activated by 1 mM GABA. Panel **B** shows the PS concentration-response relationship for receptors activated by 1 mM GABA. The data points show mean ± S.D. from 5 cells per concentration. The curve was fitted with Eq. 23, yielding a Q of 0.31 ± 0.01, K_{PS} of 3.5 ± 1.2 μM, and c_{PS} of 0.054 ± 0.014. The number of binding sites for PS was held at 1. The term $L\Gamma_{GABA}$ was constrained to 0.10 (see text). The inset more clearly demonstrates the incomplete block, also predicted by Eq. 23, at high concentrations of PS. Panel **C** shows a sample current trace demonstrating the effect of 10 μM PS on receptors activated by 3 μM GABA. Panel **D** shows the PS concentration-response relationship for receptors activated by 3 μM GABA. The data points show mean ± S.D. from 5-11 cells per concentration. The relatively large error limits reflect cell-to-cell variability in responses to 3 μM GABA. The curve shows the predicted effect of PS calculated using the Q, K_{PS} and c_{PS} values determined in the presence of 1 mM GABA (Panel B), and $L\Gamma_{GABA}$ constrained to 29. There were no free parameters in generating the predicted line in Panel D.

Figure 7. Independence of the actions of GABAergic agents. Panel **A** shows the ratio of steady-state to peak open probability as a function of peak open probability. The solid line shows the predicted relationship using Eq. 4 with Q constrained to 0.3. Small data points show the data from individual cells. Large data points show mean ± S.D. for 30 mM β-alanine (filled circle; n = 8 cells), combinations of 3-10 μM GABA + 0.1-3 μM 3α5αP (open circles; n = 3-5 cells per condition), 3 μM GABA + 0.05-0.1 μM propofol (open squares; n = 5-6 cells per condition), 1-2 μM GABA + 0.1-0.15 μM 3α5αP + 5 μM propofol (filled squares; n = 6-8 cells per condition), 1 mM GABA + 1 μM 3α5αP (triangle; n = 6 cells),1 mM GABA + 20 μM propofol (inverted triangle; n = 5 cells), and 1 mM GABA + 50 μM pentobarbital (diamond; n = 8 cells). Panel **B** summarizes the effect of 0.5 μM PS on steady-state current elicited by 1 mM GABA + 1 μM 3α5αP (circle; n = 4 cells), 1 mM GABA + 5 μM propofol (square; n = 7 cells), or 1 mM GABA + 1 μM 3α5αP + 5 μM propofol (triangle; n = 4 cells). Small data points show the data from individual cells. Large data points show mean ± S.D. The solid line shows the predicted effect of 0.5 μM PS at various steady-state open probabilities. The prediction was made using Eq. 26, with K_{PS} constrained to 3.5 μM and c_{PS} constrained to 0.054. The dashed line indicates the zero effect line.

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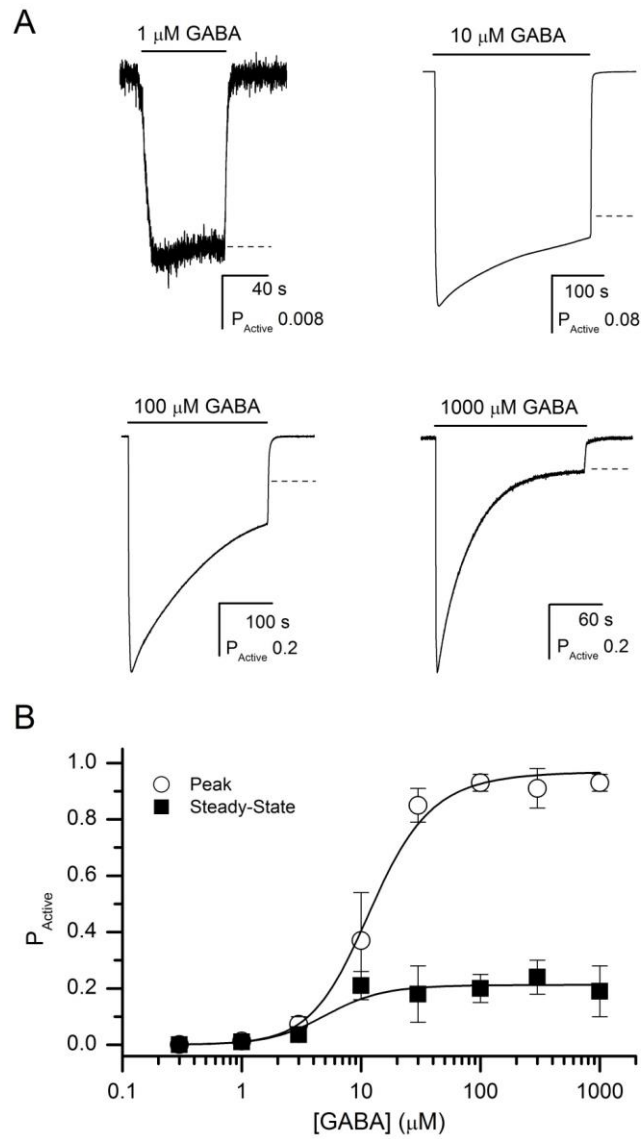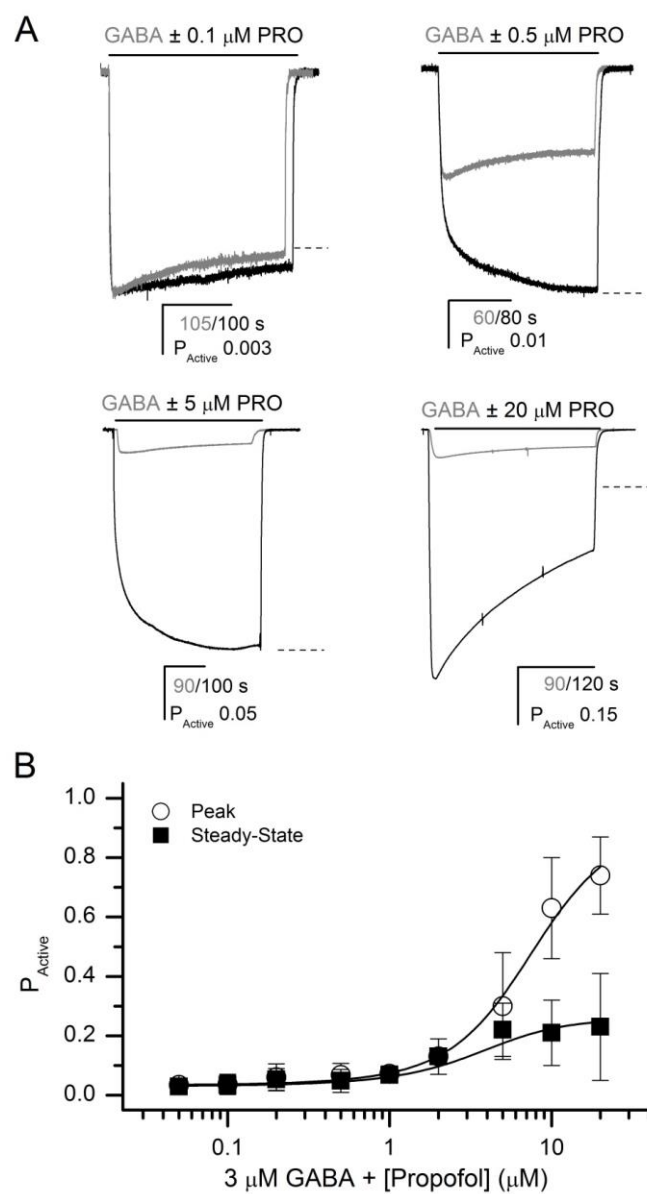
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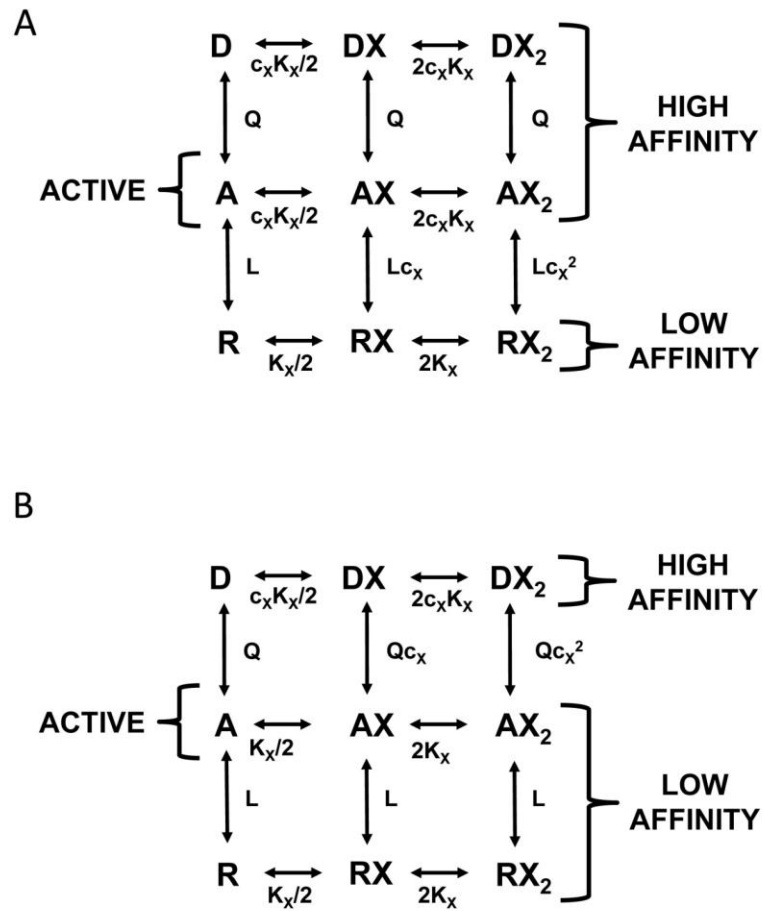
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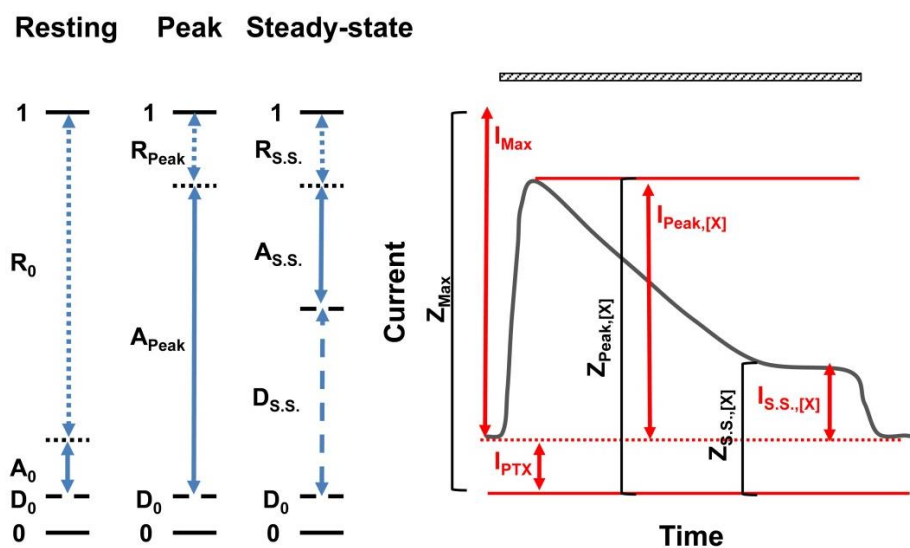
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