Heteropoda toxin 2 interaction with Kv4.3 and Kv4.1 reveals differences in gating modification

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Running title: Voltage-dependence of HpTx2 interaction with Kv4.1 and Kv4.3

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Text:

40 pages
3 tables
7 figures
36 references
249 words in the Abstract
734 words in the Introduction
1485 words in the Discussion

Abbreviations: HpTx2: Heteropoda toxin 2; TMS: transmembrane segment; VSD: voltage-sensor domain.
Abstract

Kv4 (Shal) potassium channels are responsible for the transient outward K⁺ currents in mammalian hearts and central nervous systems. Heteropoda toxin 2 (HpTx2) is an inhibitor cysteine knot peptide toxin specific for Kv4 channels that inhibits gating of Kv4.3 in the voltage-dependent manner typical for this type of toxin. HpTx2 interacts with four independent binding sites containing two conserved hydrophobic amino acids in the S3b transmembrane segments of Kv4.3 and the closely related Kv4.1. Despite these similarities, HpTx2 interaction with Kv4.1 is considerably less voltage dependent, has smaller shifts in the voltage dependences of conductance and steady-state inactivation, and a 3-fold higher $K_d$ value. Swapping four non-conserved amino acids in S3b between the two channels exchanges the phenotypic response to HpTx2. To understand these differences in gating modification, we constructed Markov models of Kv4.3 and Kv4.1 activation gating in the presence of HpTx2. Both models feature a series of voltage-dependent steps leading to a final voltage-independent transition to the open state, and closely replicate the experimental data. Interaction with HpTx2 increases the energy barrier for channel opening by slowing activation and accelerating deactivation. The greater degree of voltage-dependency in Kv4.3 occurs because it is the voltage-dependent transitions that are most affected by HpTx2; in contrast, it is the voltage-independent step in Kv4.1 that is most affected by the presence of toxin. These data demonstrate the basis for subtype specificity of HpTx2 and point the way to a general model of gating modifier toxin interaction with voltage gated ion channels.
Introduction

Potassium currents with fast activation and inactivation kinetics are present in many mammalian tissues, and are often conducted by the three members of the Shal (Kv4) family of voltage-gated K⁺ channels (Birnbaum et al., 2004). These channels are best known for their key roles in cardiovascular and nervous systems. Kv4.2 and Kv4.3 are the pore-forming channel subunits of the fast recovering cardiac transient outward current that is most prominently found in the atria, right ventricle, and left ventricular epicardium of many mammals, where their prominent role in early repolarization influences calcium current magnitude and myocardial contractility (Nerbonne and Kass, 2005). In neurons, they are responsible for the Iₐ K⁺ current in the somatodendritic region, which limits the amplitude and accelerates the decay of excitatory postsynaptic action potentials, and also inhibits back propagation of depolarization in dendrites (Covarrubias et al., 2008). A physiological role for the third member of the family, Kv4.1, has not been clearly established.

The sequences of the three Kv4 channels are highly conserved; there is 87% sequence identity between voltage sensor and pore domains of Kv4.3 and Kv4.1; 95% between Kv4.3 and Kv4.2. As expected from channels with this level of conservation, they share many gating properties. In heterologous expression systems, their conductance-voltage relationships are best described by a Boltzmann function with mid-points (V₁/₂) near 0 mV; activation and deactivation are fast compared to most other voltage-gated K⁺ channels (Birnbaum et al., 2004). Inactivation of Shal channels is a complex and
relatively slow process occurring from multiple open and closed states (Bähring and Covarrubias, 2011).

Potassium currents generated by Shal channels in vivo have been identified using the closely related peptide toxins HpTx2 and HpTx3 (Sanguinetti et al., 1997; Brahmajothi et al., 1999; Himmel et al., 1999; Kassiri et al., 2002; Ramakers and Storm, 2002; Varga et al., 2004; Nerbonne et al., 2008; Liu et al., 2011). The best characterized is HpTx2, a 30 amino acid toxin originally purified from the venom of the spider Heteropoda venatoria (Sanguinetti et al., 1997). It is one of more than 300 known ion channel peptide toxins that form an “inhibitor cysteine knot” (ICK) motif, most of which have been identified in spider venom (Gracy et al., 2008). Both in vivo data and our studies using heterologously expressed channels strongly suggested that HpTx2 is specific for Kv4 channels (Zarayskiy et al., 2005). HpTx2 inhibition of Kv4.3 was voltage-dependent, shifting the threshold for activation to more depolarized potentials, speeding deactivation, and slowing inactivation (Zarayskiy et al., 2005). Alanine scanning mutagenesis showed that HpTx2 interacts with two amino acids in the S3b TMS of the VSD (DeSimone et al., 2009). These characteristics established HpTx2 as a gating modifier toxin that inhibits the channel by interfering with the movement of the voltage sensor domain during gating.

In contrast to Kv4.3, the HpTx2 induced gating modification of Kv4.1 was much less voltage dependent (Zarayskiy et al., 2005). This surprising observation led us to compare the interaction between HpTx2 and these two channels. In this study, we show that Kv4.1 and Kv4.3 share a binding site for HpTx2 in the S3b TMS, ruling out an entirely different mechanism of gating modification for the two channels. We found that
the molecular basis of differences in voltage-dependent inhibition were due to a non-conserved four amino acid region in S3b adjacent to the toxin's putative binding site. To gain insights into the mechanism responsible for difference in HpTx2 gating modification, we developed Markov models of Kv4.1 and Kv4.3 activation in the presence of HpTx2. In the absence of toxin, we propose five closed states leading to an open state. The transitions between the closed states are voltage-dependent, while the transition from the final pre-open closed to the open state is voltage-independent. To account for HpTx2 interaction, we added four toxin-bound states, and the transition rates to account for experimentally observed toxin-dependent effects. The model suggests that HpTx2 primarily effects the voltage-dependent transitions in Kv4.3, resulting in a high degree of voltage-dependent inhibition by HpTx2. In contrast, the toxin stabilizes the final pre-open closed state of Kv4.1. Because this transition is voltage-independent, there is a lower degree of voltage dependence of HpTx2-induced gating modification. These experiments show that subtle differences in the gating properties of two closely related K⁺ channels can result in large differences in gating modification by toxins or drugs that have similar molecular basis of interaction with their ion channel targets.
Materials & Methods

Preparation of RNA for Oocyte Injection. The short form of rat Kv4.3 (636 amino acids; NCBI accession NP_113927), and the mouse Kv4.1 (NP_032449) were described previously (Wang et al., 2002; Zarayskiy et al., 2005). Site directed mutagenesis was performed as described (DeSimone et al., 2009); mutant identity was confirmed by DNA sequencing. Plasmids encoding cloned channels were linearized by restriction endonuclease digestion, and transcribed using T7 RNA polymerase (mMessage Machine; Applied Biosystems/Ambion, Austin, TX, USA). The reaction was terminated by DNAase I treatment followed by precipitation of RNA with LiCl, and suspended in RNAase-free water included in the mMessage Machine kit. The sample concentration was determined by absorbance at 260 nm, adjusted to 500 ng/mL, and stored at −80°C.

Xenopus Oocyte Preparation. Use of Xenopus laevis has been considered and approved for numbers of animals, humane treatment, care, and method of euthanasia by the University at Buffalo-SUNY Institutional Animal Care & Use Committee, and was carried out in accordance with the Declaration of Helsinki and with the Guide for the Care and Use of Laboratory Animals as adopted and promulgated by the U.S. National Institutes of Health.

Oocytes were prepared as previously described (DeSimone et al., 2009). Frogs obtained from Xenopus I (Dexter, MI, USA) were anesthetized by immersion in 2.0 mM 3-aminobenzoic acid ethyl ester (Sigma-Aldrich, St. Louis, MO USA) for at least 10 min.
The ovarian lobes were harvested and placed in Ca$_{2+}$-free ND96 (mM: 96 NaCl, 2 KCl, 1 MgCl$_2$, 5 HEPES, pH 7.4) and treated with 1-2 mg/ml collagenase (Type II; Sigma-Aldrich, St. Louis, MO, USA) to remove the follicular cell layer. Oocytes were injected with 10-50 nL *in vitro* transcribed mRNA. Injected oocytes were incubated at 18°C in normal ND96 (including 1.8 mM CaCl$_2$) + antibiotic/antimycotic (Invitrogen, Carlsbad, CA, USA) for 3-7 days.

**Two-Electrode Voltage-Clamp Technique.** Currents were measured in oocytes using a two-microelectrode Dagan CA-1B amplifier as described (Wang et al., 2004; Wang et al., 2005). Electrodes were filled with 3M KCl. Experiments were performed at room temperature (20-24°C), or at 16°C where noted, in either ND96 + 0.1% BSA or 98K +0.1% BSA (98mM KCl, 1mM MgCl$_2$, 1.8mM CaCl$_2$, and 5mM HEPES, pH=7.4). For experiments performed at 16°C, a Dagan HCC-100 temperature controller was used to regulate both the recording chamber and solution temperatures. Data were digitized at either 50 kHz or 5 kHz using Clampex 9.2 (Molecular Devices, Sunnyvale, CA, USA), and analyzed with Clampfit 9.2, Microsoft Excel 2007, or Sigma Plot 9 (SSPS, Chicago, IL, USA). Raw current traces shown were neither leakage nor capacitance subtracted.

**Pulse Protocols and Data Analysis.** The holding potential for all pulse protocols was -90 mV. A two-pulse protocol was employed to measure the current-voltage (*I*-*V*), conductance-voltage (*G*-*V*), steady-state inactivation (SSIA) relationships, and time to peak current. From the holding potential, 3 s voltage steps (P1) were applied from -120 to +50 mV in 10 mV increments followed by a 1 s pulse (P2) to +50 mV, with a 3 s interval before the next P1 pulse. Normalized current (*I*/*I$_{\text{max}}$) was calculated as the ratio of the maximum current during the P1 pulse to the maximum current during the 50 mV
P1 pulse before application of HpTx2. Conductance $G(V)$ at each voltage was calculated from the equation $G(V) = \frac{I_{\text{max}^1}}{(V-E_K)}$, where $V$ is the depolarization voltage during P1, $I_{\text{max}^1}$ is the maximum current during P1, and $E_K = -100$ mV, the reversal potential of $K^+$ for *Xenopus* oocytes in ND96. The $G-V$ relationship was obtained by fitting $G(V)$, normalized to the maximal conductance value, with a Boltzmann function $f_a(V) = \frac{G_{\text{max}}}{1 + \exp\left[\frac{(V_{1/2} - V)}{k}\right]}$, where $V_{1/2}$, $k$, and $G_{\text{max}}$ are the half-activation potential, the slope-factor, and 1.0, respectively. Steady-state inactivation was determined as the ratio of the maximum current during P2, $I_{\text{max}^1}$, for the P1 depolarization voltage to the maximum value of $I_{\text{max}^2}$. The voltage dependence of steady-state inactivation relationships were fitted by the Boltzmann function $f_i(V) = \frac{1}{1 + \exp\left[\frac{(V_{1/2,i} - V)}{k_i}\right]}$, where $V_{1/2,i}$ and $k_i$ are the half-inactivation potential and the slope factor, respectively.

Association/dissociation experiments (Fig. 2A and Fig. 3, J-K) were performed with a two pulse protocol: the P1 pulse was to −10 mV for 12 ms, followed by a P2 pulse to −50 mV for 150 ms, with a 1 s interpulse interval. The data represent the normalized reciprocal current amplitude measured from the maximum of the P2 pulse. The on and off rates were fit with the functions $f_{\text{on}}(t) = C \times \exp(-t/4\tau_{\text{on}})$ and $f_{\text{off}}(t) = C \times \left[1 - \exp(-t/\tau_{\text{off}})\right]^4$, respectively. The dissociation constants $(K_d) = k_{\text{off}}/k_{\text{on}}$, where $k_{\text{off}} = 1/\tau_{\text{off}}$ and $k_{\text{on}} = 1/(4 \times [HpTx2] \times \tau_{\text{on}})$.

Activation was measured using a series of 1000 ms pulses from the −90 mV holding potential to a series of steps from −30 to +50 mV in 10 mV increments. The activation time constants were determined by fitting the activation time course to the function $f_{\text{act}}(t) = C \times (1 - \exp[-t/\tau_{\text{act}}])^4$. To measure deactivation, the P1 pulse was set to +50 mV for 12 ms, followed by a 150 ms P2 pulse from −120 to −40 mV in 10 mV increments.
Deactivation time constants were determined by fitting the currents in the P2 pulse to the function $f_{\text{deact}}(t) = C \times (1-\exp[-t/\tau_{\text{deact}}])$.

**Model development.** Model development was performed on a DEC alpha workstation using Fortran 90. The Markov model was implemented as a set of evolution differential equations for five closed states, $C_0$-$C_4$, and one open state, $O$. The numerical solution of differential equations was performed by a fourth-order Runge-Kutta method. Channel models were allowed to run for at least 600 seconds to calculate the steady-state values of occupancies of channel states, and were used as the initial conditions (Wang et al., 2004).
Results

Gating modification of Kv4.1 by HpTx2

Peptide toxins have found wide use as structural probes for ion channels and as pharmaceutical agents (Lewis and Garcia, 2003; Catterall et al., 2007; Estrada et al., 2007; Swartz, 2007; Hodgson and Isbister, 2009; Dutertre and Lewis, 2010). Their interaction with ion channels falls into two general classes: pore blockade or gating modification. Pore-blocking toxins bind to the pore region of a channel and prevent permeation of ions through occlusion of the external channel pore. Gating modifier toxins inhibit or activate ion channel conductance by interfering with the energetics of channel gating (Catterall et al., 2007; Swartz, 2007).

A hallmark of gating modifier toxin activity on voltage-gated K+ channels is voltage-dependent inhibition; there is a greater degree of channel inhibition at voltages near the activation threshold (Swartz and MacKinnon, 1995). This effect can be seen by comparing the I-V relationships of Kv4.3 in the presence and absence of 2 μM HpTx2 (Fig. 1A). Note that at voltages less than 0 mV, there is a much greater degree of channel inhibition than at higher voltages, indicating strong voltage-dependent inhibition. Kv4.1 is a close relative of Kv4.3, with more than 90% amino acid identity from the beginning of S1 to the end of S6. However, inhibition of Kv4.1 by HpTx2 exhibited less voltage dependence (Fig. 1B). For example, at 0 mV 80% of the Kv4.3 current is inhibited, while Kv4.1 current is only reduced by half. In contrast, at +50 mV, 2 μM HpTx2 inhibits both channels to nearly the same degree; 38% of Kv4.3 current is
inhibited vs. 36% of the Kv4.1 current (Fig. 1, A-D). This manifests itself in relatively
feeble shifts in the normalized conductance-voltage relationship \((G-V)\) when toxin is
applied to Kv4.1; the change in voltage at one half the maximum normalized
conductance \((\Delta V_{1/2})\) values are 22.0 ± 1.6 mV and 10.2 ± 1.2 mV for Kv4.3 and Kv4.1,
respectively (Fig. 1, E-F, and Table 1). Similar differences were observed in the voltage
dependences of steady-state inactivation, with Kv4.3 having much larger shifts in
voltage dependency than Kv4.1 (Fig. 1, G-H, and Table 1).

Kv4.3 and Kv4.1 also showed differences in their apparent affinity for HpTx2. To
determine the gating modification kinetics and apparent dissociation constant we used a
method described in detail elsewhere (Swartz and MacKinnon, 1997; DeSimone et al.,
2009). Briefly, we used a two pulse protocol from our previously determined threshold
depolarization voltages of −10 mV to −50 mV at 1 s intervals. The bath solution
contained 98 mM K⁺ to ensure sufficiently large tail current amplitudes to accurately
measure the toxin occupancy. After establishing baseline current amplitude, toxin was
applied directly to the chamber. When toxin inhibition reached steady state, the toxin
was washed off the oocyte by perfusion (Fig. 2, A). The time courses of association and
dissociation were fit with exponential functions; dissociation was fit with a forth power
exponential function to account for the four-fold symmetry of Kv4.1, which suggests four
HpTx2 binding sites, as was established for HpTx2 interaction with Kv4.3 (DeSimone et
al., 2009). The \(K_d\) of HpTx2 was 7.1 ± 1.1 μM (Table 2), roughly 3-fold higher than the
2.3 ± 0.3 μM of HpTx2 with Kv4.3.

HpTx2 inhibition of Kv4.3 occurs by gating modification through a putative binding site in
S3b (DeSimone et al., 2009), however, the relative lack of voltage-dependence
observed in the Kv4.1 I-V suggested that HpTx2 might somehow be occluding the pore of this channel. Given the apparent structural similarity between Kv4.1 and Kv4.3, this would likely mean that the channels do not share the same toxin binding site, which in turn would suggest a different mechanism of channel inhibition. Previously, we found that the critical amino acids necessary for toxin-channel interaction in Kv4.3 were a leucine and valine at positions 275 and 276 (DeSimone et al., 2009). The amino acids at the analogous positions in Kv4.1 are a leucine and a phenylalanine (Fig. 2B). Therefore, we constructed Kv4.1 [(L275,F276)A], substituting the two amino acids at positions 275 and 276 with alanine, similar to the modification which nearly eliminates Kv4.3 interaction with HpTx2 (DeSimone et al., 2009). When expressed in *Xenopus* oocytes, the mutant Kv4.1 expressed currents similar to the wild-type Kv4.1. However, there is almost complete loss of gating modification after application of 5µM HpTx2 (Fig. 2, C-D, and Table 1). These data show that the putative binding site of HpTx2 is the same in Kv4.3 and Kv4.1, strongly suggesting that the differences in gating modification are due to intrinsic differences in gating between the two channels and not by the location of toxin binding.

**Differences in the S3b TMS account for the difference in gating modification**

While putative binding site differences between Kv4.3 and Kv4.1 do not account for the differences in channel behavior toward HpTx2, other amino acid differences could account for this phenomenon. Aside from the typically non-conserved S1-S2 TMS external linker, the largest stretch of different amino acids in the voltage sensor and pore domains stretches from amino acid V276 to N279 in Kv4.3, and F276 to K279 in
Kv4.1 (Fig. 2B). Proximity to both the apparent HpTx2 binding site on Kv4.3 and the S4 transmembrane voltage-sensing sequence suggested that these amino acids might be important in determining the gating modification behavior of Kv4 channels in response to HpTx2. Therefore, we swapped amino acids 276-279 between Kv4.1 and Kv4.3 to give the mutant channels Kv4.1 [276VMTN] and Kv4.3 [276FVPK], and tested their response to application of 2 μM HpTx2.

In the absence of toxin, the Kv4.3 and Kv4.1 mutants retain the basic current phenotype of their wild-type precursors (Fig. 3, A, E, compare to Fig. 1, C, D). Note that the V½ and k values for G-V and SSIA are nearly identical between wild type Kv4.1 and Kv4.1 [276VMTN], and likewise between wild type Kv4.3 and Kv4.3 [276FVPK] (compare Fig. 1, A, B, E-H, to Fig. 3, B-D and F-H; see Table 1). However, application of HpTx2 revealed dramatic differences between the wild type and mutant phenotypes of the two channels. Kv4.1 [276VMTN] behaves toward 2 μM HpTx2 very similarly to wild-type Kv4.3 (Table 1). Like wild type Kv4.3, the Kv4.1 S3b mutant has a high degree of voltage sensitivity toward toxin inhibition; 2 μM HpTx2 inhibits 39% and 82% of the Kv4.1 [276VMTN] current at 50 mV and 0 mV, respectively (Fig. 3B). The behavior of Kv4.1 [276VMTN] + 2 μM HpTx2 with respect to G-V is not identical to Kv4.3, but still much more like Kv4.3 than Kv4.1 (Fig 3E). The ΔV½ of the G-V for Kv4.1 [276VMTN] is 32.1 ± 2.4 mV compared to 22.0 ± 1.6 mV for Kv4.3 and 10.2 ± 1.2 mV for Kv4.1. Similarly, the shift in voltage-dependence of Kv4.1 [276VMTN] SSIA is nearly identical to that of Kv4.3; ΔV½ = 16.0 ± 0.02 for Kv4.1 [276VMTN] and 18.4 ± 2.1 for Kv4.3 (Fig. 3, C, I).
The reciprocal mutation, Kv4.3 [276FVPK], provides a mirror image of Kv4.1 [276VMTN]. In all respects, Kv4.3 [276FVPK] in the presence of HpTx2 behaves much more like wild type Kv4.1 than Kv4.3. Kv4.3 [276FVPK] is 31% inhibited by 2 μM HpTx2 at +50 mV, and 49% inhibited at 0 mV, close to the values of 36% and 54% obtained with wild type Kv4.1 (Fig. 3F). Likewise the ΔV½ values for G-V and SSIA are all very close: 9.7 ± 0.7 mV, and 3.5 ± 0.09 mV for Kv4.3 [276FVPK], compared to 10.2 ± 1.2 mV, and 2.3 ± 0.06 mV for Kv4.1 (Fig. 3, G, H; summarized in Fig. 3I, and Table 1). This pattern also holds for the kinetics of gating modification and Kd (Fig. 3, J-K; Table 2), with the k_on, k_off, and Kd of Kv4.3 [276FVPK] being close to those of Kv4.1, while the same parameters determined for Kv4.1 [276VMTN] are very close to those of wild type Kv4.3. Taken together, these data show that four amino acids in S3b are capable of reversing the HpTx2 interaction phenotype of Kv4 channels between voltage-sensitive inhibition seen in Kv4.3 and the relatively voltage-insensitive interaction typical of Kv4.1.

**Kinetic modeling of HpTx2 interaction with Kv4.1 and Kv4.3**

The previous experiments allowed us to deduce the molecular basis of the differences in HpTx2-induced gating modification of Kv4.1 and Kv4.3. However, these data do not address the functional basis for these differences. Conservation of the HpTx2 binding site in the two channels suggests that the answer does not lie in the mechanism of toxin interaction with the channel, but in differences of its effect on activation and deactivation of Kv4.1 and Kv4.3.

To test this hypothesis, we took our previously described Markov model of Kv4.3 activation (Wang et al., 2004), and used experimentally derived data to develop a Markov model of Kv4.1 activation. The Markov model structure for activation in the
absence of HpTx2 is described in Scheme 1 (Fig. 4A). It includes four closed states (C₀-C₃), a pre-open closed state (C₄), and an open state (O). Transitions between the closed states are voltage-dependent. The C₄ to O transition is voltage-independent. Kv4.1 and Kv4.3 have four subunits, and the model assumes that each subunit must be activated before the channel can conduct ions. The model parameters are described in Table 3.

We obtained the rate constants for Kv4.3 and Kv4.1 model development based on experimental results from the voltage dependence of activation, deactivation, and G/G_max. These experiments were performed at 16°C to slow the activation and deactivation rates, which kept signals from being obscured by the capacitance transient, allowing accurate assessment of τ_act and τ_deact (Fig. 5, A-B). The model simulates the voltage dependence of τ_act and τ_deact that are well fit to the experimental data (Fig. 5, C-F). The forward rate constants (α) and voltage independent rate constants (k_co and k_oc) are the same in both models. Deactivation is slower in Kv4.1 than Kv4.3 (τ_deact, Kv4.1 = 7.2 ± 0.3 ms⁻¹, and 4.8 ± 0.3 ms⁻¹ for Kv4.3, both at −120 mV; Fig. 5, E, F); to account for this, we reduced the reverse rate constant (β) by a factor of 0.82 in Kv4.1 (Table 3).

Because the toxin binding experiments were conducted at room temperature (about 21°C), the derived values of the forward (α) and reverse (β) rate constants at 16°C were multiplied by the square root of the Q₁₀ (3.17 ± 0.54; (Campbell et al., 1993)) to compensate for temperature differences. This compensation gives similar results obtained during development of our original Kv4.3 model (Wang et al., 2004), suggesting that it is valid for Kv4.1 activation as well. To model the effect of HpTx2 on Kv4.1 and Kv4.3, we assumed that one toxin molecule could bind to each subunit and
that each subunit activates independently. This results in independent modification of the transition rates for activation-deactivation of toxin-bound subunits. Combining the activation model of Scheme 1 (Fig. 4A) with a kinetic model for toxin binding (Swartz and MacKinnon, 1997), we constructed a 30-state Markov model for toxin-channel interaction illustrated in Scheme 2 (Fig. 4B). In this model, each closed state can be occupied by up to four toxin molecules. At –90 mV, HpTx2 binds to the closed state of Kv4 channels; these closed states have four “non-activated” subunits through the toxin binding pathway from C0 to CB04 (see Fig. 2, A, and DeSimone, et al. (2009); transitions C0 to CB04 in Fig. 4, B with rates kon and koff). This gives the models five subpopulations of channels whose activation pathways can accommodate up to four bound toxin molecules. Activation and deactivation kinetics of the channels are roughly 3 orders of magnitude faster than toxin on and off rates, strongly suggesting that the channels will retain bound toxin in the open state. This is shown in the model as one unbound open state O, and four open states with bound toxin (OB1-OB4, Fig. 4B).

To determine transition rates between states in the Markov model, we used experimental data of the influence of HpTx2 on Kv4.3 and Kv4.1 I-V and G-V relationships, activation and deactivation kinetics. The models postulate that binding of one toxin molecule changes the activation and deactivation rate constants for each channel subunit. For example, when one toxin molecule is bound to the channel, the total transition rate from CB01 to CB11, is \( \alpha_T + 3\alpha \) (Fig. 4B). There are 12 possible transitions from CB11 to CB21 (two activated subunits); 3 with a rate of \( \alpha_T \) and 9 with rates equal to \( \alpha \), yielding a net transition rate of \( \frac{3}{4}(\alpha_T + 3\alpha) \). Similarly, deactivation rate constants from CB21 to CB11 to CB01 are \( \beta_T + 3\beta \) and \( \frac{3}{4}(\beta_T + 3\beta) \), respectively. Identical
reasoning was used to assign the voltage-dependent rate constants to the remainder of the transitions in Scheme 2.

The rules are similar for voltage-independent transitions. The modified transition rates for each subunit (\(k_{cOT}\) and \(k_{oCT}\)), result in the voltage-independent rates

\[
\frac{1}{4}\left[ k_{cOT} + (4-i)k_{CO}\right]
\]

and

\[
\frac{1}{4}\left[ k_{oCT} + (4-i)k_{OC}\right],
\]

where “\(i\)” is the number of toxin molecules bound to the channel.

The association and dissociation rates between toxin-bound states with at least one activated subunit were modified to fulfill the conditions of detailed thermodynamic equilibrium. For example, for transitions between CB\(_{11}\) and CB\(_{12}\), coefficients \(t_{a2}\) and \(t_{b2}\) are defined as:

\[
t_{a2} = \frac{2\alpha_T + 2\alpha}{\alpha_T + 3\alpha} \quad \text{and} \quad t_{b2} = \frac{2\beta_T + 2\beta}{\beta_T + 3\beta}
\]

which result in equal clockwise and counter-clockwise products of rate constants between states CB\(_{01}\), CB\(_{11}\), CB\(_{12}\), and CB\(_{02}\). Similarly, from detailed thermodynamic equilibrium we can define coefficients \(t_{cOT2}\) and \(t_{oCT2}\) as:

\[
t_{cOT2} = t_{a2}\frac{2k_{cOT} + 2k_{CO}}{k_{cOT} + 3k_{CO}} \quad \text{and} \quad t_{oCT2} = t_{b2}\frac{2k_{oCT} + 2k_{OC}}{k_{oCT} + 3k_{OC}}
\]

for the transitions between CB\(_{41}\), OB\(_{1}\), OB\(_{2}\), and CB\(_{42}\). All rate other constants for the 30-state Markov model can be found in Figure 4B.

The rate constants that were changed to account for HpTx2 interaction with Kv4.1 and Kv4.3 are summarized in Table 3. Application of 2 \(\mu\)M rHpTx2 increased the time-to-peak current by 10% and 20% at for Kv4.1 and Kv4.3, respectively (Fig. 5, G-H), making the activation rate constants \(\alpha_T = 0.9\alpha\) for Kv4.1 and \(\alpha_T = 0.8\alpha\) for Kv4.3.
Deactivation of both channels accelerated by a factor of two, so that $\beta_T = 2\beta$ for both Kv4.1 and Kv4.3. To account for the differences in the toxin effect on current-voltage and conductance-voltage relationships (Fig. 1, A-F), the values of $k_{cot}$ were reduced to 5400 s$^{-1}$ and 4000 s$^{-1}$ for Kv4.1 and Kv4.3, respectively, from 6000 s$^{-1}$ without toxin. Likewise, $k_{oct}$ was increased from 1500 s$^{-1}$ without toxin to 9000 s$^{-1}$ and 3000 s$^{-1}$.

The Markov model of Kv4.3 and Kv4.1 activation incorporating HpTx2-bound states produces simulated data that gives the optimized fits to the experimental data. The model predicts that the $k_{on}$ at 5 μM HpTx2 for Kv4.1 is 6490 M$^{-1}$·s$^{-1}$ and a $k_{off}$ of 0.0286 s$^{-1}$, compared to the experimentally determined 5000 ± 650 M$^{-1}$·s$^{-1}$ and 0.0355 ± 0.0029 s$^{-1}$, respectively, giving a predicted $K_d$ of 4.4 μM compared to the experimentally determined 7.1 ± 1.1 μM. Likewise, the predicted $k_{on}$, $k_{off}$, and $K_d$ of 2 μM HpTx2 for Kv4.3 were 13020 M$^{-1}$·s$^{-1}$, 0.0120 s$^{-1}$, and 0.92 μM, compared to the experimentally determined values of 8450 ± 1140 M$^{-1}$·s$^{-1}$, 0.0193 ± 0.00011 s$^{-1}$, and 2.3 ± 0.3 μM, respectively (Fig. 6A, and Table 1). In both cases, the predicted $K_d$ is about 2-fold lower, however, the affinity constants maintain their relative values with respect to the two channels.

In developing the model, we made minimal changes to the specified parameters based on the experimental data. Changing other gating parameters did not produce a model that fit experimental data. Specifically, changes in rate constants ($\alpha$ and $\beta$) of the voltage-dependent steps of the Kv4.1 activation model created shifts in the normalized G-V relationship that did not fit the experimental data; the changes in $k_{OC}$ were the only variation we found that mimicked the effects of HpTx2.
Likewise, the simulated data of the toxin’s influence on the current, and conductance-voltage relationships reproduced the experimental data well. The outstanding difference in HpTx2-induced I-V relationships between Kv4.3 and Kv4.1 was the degree of voltage-dependent inhibition. The model predicts that 2 μM HpTx2 will inhibit 53% of Kv4.1 K⁺ current at 0 mV, and only 31% at 50 mV, compared to the experimental data of 54 ± 5% and 36 ± 2 %, respectively (Fig. 6B). For Kv4.3 inhibition at 0 mV, the model predicts 81% compared to the measured value of 80 ± 3%, and at 50 mV, 45% compared to the measured value of 37 ± 3% (Fig. 6C). The ΔV½ in G/Gmax for Kv4.1 upon application of 2 μM HpTx2 was 10.2 ± 1.2 mV, close to the 16.3 mV predicted by the model. Under the same conditions, Kv4.3 shifts 22.0 ± 1.6 mV, about 3 mV less than the predicted 24.9 mV shift (Fig. 6, D-E). These close approximations suggest that the observed differences in Kv4.1 and Kv4.3 gating upon HpTx2 application are due to differences in modification of the kinetics of both the voltage-dependent and voltage-independent transitions occurring during channel activation and deactivation.
Discussion

*Heteropoda* toxin 2 is one of many ICK toxins that are voltage-dependent gating modifiers of mammalian voltage-gated K⁺ channels (Swartz, 2007). However, HpTx2 is the first K⁺ gating modifier toxin to show the type of isoform-specific voltage-dependent properties demonstrated by our data. To understand this novel observation, we identified the molecular basis of the differences in gating modification of Kv4.3 and Kv4.1 by HpTx2. We then developed a 30 state Markov model that can account for how the toxin influences the two channels differently. To our knowledge, this is the first detailed study to examine the mechanism of these differences, and to apply this knowledge to enhance our understanding of Kv4 channel gating.

The model accounts for the difference in voltage-dependent inhibition between Kv4.1 and Kv4.3 by HpTx2. Experimental data showed about a 3-fold difference in apparent Kₐ for HpTx2 binding to the two channels (Table 2). The larger Kv4.1 Kₐ results in a smaller number of toxin-bound channels in the C₀₁ to C₃₄ states at any given voltage; therefore, more channels follow the direct activation pathway from C₀ to O. The result is the comparatively small depolarizing shift in Kv4.1 G-V in the presence of toxin. However, Kv4.1 and Kv4.3 are inhibited by toxin to nearly the same degree at +50 mV. To account for this, we increased the toxin-bound voltage-independent rate (kₒc) 2-fold in the Kv4.3 model and 6-fold in the Kv4.1 model, resulting in a more stable Kv4.1 C₄ state. The higher affinity of HpTx2 for Kv4.3 results in greater inhibition during the voltage-dependent steps. Therefore, a smaller decrease in kₒc gives the same degree of inhibition of Kv4.3 by HpTx2.
The probabilities of finding Kv4.1 and Kv4.3 in the presence of toxin in closed and open states (state occupancies) are illustrated in Figure 7. At −50 mV, below the threshold for activation, both channels are in the C₀-C₃ states regardless of HpTx2. As the voltage increases to −10 mV in the absence of toxin, a significant fraction of channels open: 29% of Kv4.1 (Fig. 7A) and 16% of Kv4.3 (Fig. 7B); only 7% of Kv4.1 and 4% of Kv4.3 occupy the C₄ state (Fig. 7C). With the addition of 2 μM HpTx2, a negligible number of Kv4.3 channels are in the open and C₄ states at −10 mV. However, a significant fraction of Kv4.1 channels are open (13%) and in the C₄ (8%) states under these conditions, which is reflected the lower degree of voltage-dependence of HpTx2 interaction with Kv4.1. At +30 mV in the absence of HpTx2, the two channels have about the same proportion of open, C₀-C₃, and C₄ states. In the presence of toxin, the number of open state channels are decreased in favor of closed states for both channels, however, the fraction of Kv4.1 in C₄ state is 24% compared to only 10% of Kv4.3. The relatively large effect of HpTx2 on the voltage-independent transition from C₄ to O of Kv4.1 results in higher occupation of the C₄ state, thus accounting for the low degree of voltage dependence of HpTx2 modification of Kv4.1 gating.

In developing models to account for the effects of HpTx2 on Kv4.3 and Kv4.1, we restricted ourselves to a description of the toxin’s effects on Kv4.3 and Kv4.1 activation. Eliminating inactivation from our models of HpTx2 gating modification is possible because all forms of inactivation in Kv4.1 and Kv4.3 are much slower than activation and deactivation in the presence of HpTx2. These rate differences allow measurement of activation and deactivation at time scales that do not allow significant development of inactivation.
Eliminating inactivation also greatly simplified model development, while still allowing us to account for our experimental observations. This is not surprising; aside from the long time constants involved in inactivation, our previous studies showed that HpTx2 has very modest effects on Kv4 inactivation kinetics (Zarayskiy et al., 2005). Further, the shifts in $V_{1/2}$ steady-state inactivation induced by HpTx2 (Fig. 1, G-H) mirror the shifts in $V_{1/2}$ calculated from the $G-V$ relationship, the result being a much smaller $\Delta V_{1/2}$ for Kv4.1 than for Kv4.3 ($\Delta V_{1/2,SSIA}=2.3 \pm 0.06$ mV for Kv4.1 and $18.4 \pm 2.1$ mV for Kv4.3; Table 1). This behavior probably reflects the coupling of Kv4 inactivation to activation. While a full consideration of inactivation in our Markov models might have contributed some insight to Kv4 inactivation, our goal was to understand the differences in behavior observed between Kv4.3 and Kv4.1 in the presence of HpTx2. The success of our model in recapitulating our experimental data argues that the assumptions behind its development (i.e. not including inactivation) are valid and that inactivation is not important to understanding our observations.

Our previous work has shown that the critical amino acids for HpTx2 gating modification of Kv4.3 are a leucine and valine dyad at amino acid 275 in transmembrane segment S3b (DeSimone et al., 2009). In Kv4.1, the required amino acids are a conserved leucine and a phenylalanine at the homologous position in S3b (Fig. 2B). In addition to the binding sites being similar, we have also shown that the number of potential binding sites between the two channels is identical. However, the most striking feature of HpTx2 interaction with Kv4.3 and Kv4.1, is the difference in the degree of voltage sensitive inhibition. We have established that this effect is solely due to four non-identical amino acids in S3b that overlap with the HpTx2 binding site. Individual point mutations of the
four non-conserved amino acids had little effect on voltage dependency, except for P278T (in Kv4.1; data not shown), whose effects were similar, but not as dramatic as those of Kv4.3[276FVPK] and Kv4.1[276VMTN] which effectively reversed the gating modification phenotype (Fig. 3). The existence of proline 278 in Kv4.1 is unique; there are no other occurrences at the homologous position in any known voltage-gated K+ channel. The S3b of Kv2.1 forms an α helix through this position (Long et al., 2007), however, proline is well-known for its inability to fit into internal positions in helices, and is most often associated with turns (Richardson and Richardson, 1989), suggesting the structure of Shal channel S3b may not be well conserved with Kv2.1.

Gating-modifier toxins similar to HpTx2 interact with the outward facing portion of the VSD, sitting between the VSD and the pore domain, where they are well positioned to interfere with the translational and rotational movement of the VSDs that lead to opening of the channel pore (Milescu et al., 2009; Wee et al., 2010). The VSD has been implicated in the transition from the voltage independent pre-open closed state (C4) to the open state (Schoppa and Sigworth, 1998; Zandany et al., 2008). We show that much of the inhibition of Kv4.1 by HpTx2 must be occurring during this final, voltage-independent step, suggesting an important role for S3b movement in the transition. Alternatively, the different S3b sequence of Kv4.1 might allow HpTx2 to interfere with the concerted conformational changes in each pore domain subunit required for channel opening. While we lack the structural data required to distinguish these hypotheses, we believe that this study emphasizes the unique value of gating modifier toxins in understanding activation kinetics and their relation to voltage-sensor structure and movement in voltage-gated ion channels.
HpTx2 is one of 18 peptide toxins reported to interact with a member of the Kv4 family (Herzig et al., 2011), all of which share the inhibitor cysteine knot tertiary structure and were purified from spider venom. Of these, three others have been shown to discriminate between Kv4.3 (or Kv4.2) and Kv4.1, while not interacting with other voltage-gated channels. Two were purified from the *Phrixotrichus auratus* venom, PaTx1 and PaTx2, with PaTx1 being the more potent of the two (Diochot et al., 1999); these toxins share about 50% sequence identity with HpTx2. PaTx1 inhibition of Kv4.3 is similar to that of HpTx2 except that it significantly slows inactivation kinetics and recovery from inactivation. It is also a weaker inhibitor of Kv4.1 currents. In contrast, A toxin 79% identical to PaTx1, JZTX-XII purified from *Chilobrachys jingzhao* venom, is a relatively strong inhibitor of Kv4.1, and a much weaker inhibitor of Kv4.2 (Yuan et al., 2007); HpTx2 inhibits Kv4.2 to roughly the same degree as Kv4.3 (Zarayskiy et al., 2005). While it is likely these three toxins interact with Kv4 channels at or near the S3b HpTx2 binding site, this assumption has not been tested experimentally. Previously, we have shown differences in the affinity of HpTx2 for Kv4.3 associated with an ancillary subunit (DeSimone et al., 2009), in this work we have shown how to distinguish Kv4.1 currents from Kv4.3 (and likely Kv4.2) currents using this toxin. While we have not tested all combinations of Kv4 channel and ancillary subunit for their current phenotype in response to HpTx2, we believe that this toxin, perhaps in combination with other Kv4-specific peptide toxins, will prove to be useful in unambiguous identification of the molecular basis of transient outward K⁺ currents.
Acknowledgements

The authors wish to thank Dr. Chang Xie for preparation of oocytes, YiChun Lu for preparation of RNA, Dr. Larry Salkoff for his gift of the Kv4.1 construct, and Dr. Randall Rasmusson for advice, support and encouragement.
Author Contributions

Participated in research design: DeSimone, Bondarenko, Morales

Conducted experiments: DeSimone, Zarayskiy

Contributed new reagents or analytic tools: Bondarenko, Morales

Performed data analysis: DeSimone, Zarayskiy, Bondarenko, Morales

Wrote or contributed to the writing of the manuscript: DeSimone, Bondarenko, Morales
References


Footnotes

**Funding.** This work was supported by a Scientist Development Grant, a Predoctoral Fellowship, and a Grant-in-aid from the Founders, and Southeast Affiliates of the American Heart Association [Grants 0235500T, 0615662T, 10GRNT4720012], the John R. Oishei Foundation, and a Georgia State University Brain and Behavior Research Initiation Grant.

This work was presented previously in abstract form at the 55th annual meeting of the Biophysical Society in Baltimore, MD, March 5-9, 2011 (*Biophys J* **100**:283a, Supplement 1), and as a portion of the doctoral thesis of CV DeSimone (2009; University at Buffalo, the State University of New York).

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Figure Legends

Figure 1. Kv4.3 and Kv4.1 react differently to application of 2 μM HpTx2. Plots of Kv4.3 are on the left; all panels with Kv4.3 use circles. Kv4.1 is in the right column; all plots use squares. Closed symbols with black lines represent the controls, while open symbols with gray lines represent the result of HpTx2 application. These conventions are maintained throughout this work. The pulse protocols and fitting algorithms (E-H) are described in Materials and Methods. All panels except C and D are shown as the mean ± S.E.M., n=5-6. (A) Current-voltage relationship of Kv4.3 ± HpTx2. (B) Current-voltage relationship of Kv4.1 ± HpTx2. (C-D) Representative current traces of Kv4.3 and Kv4.1 in the presence of HpTx2 (gray). Currents were elicited from a holding potential of −90 mV to 0 mV for 2.5 seconds. The scale bars represent 0.5 μA × 0.5 s. The data was neither leakage nor capacitance subtracted. (E-F) Conductance-voltage relationships of Kv4.3 and Kv4.1 in the presence of HpTx2. (G-H) Voltage-dependence of steady-state inactivation of Kv4.3 and Kv4.1 in the presence of HpTx2. Note in panels E and G that Kv4.3 has robust changes in voltage dependence to more depolarized potentials after application of HpTx2, a response characteristic of gating modifier toxins. In contrast, the same concentration of HpTx2 induces relatively feeble voltage-dependent effects in Kv4.1 (see Table 1).

Figure 2. The apparent HpTx2 binding site in the Kv4.3 S3b TMS is conserved in Kv4.1. (A) Determination of the apparent Kd value of HpTx2 for Kv4.1 as described (DeSimone et al., 2009). The pulse protocol and fitting algorithm are described in
**Materials and Methods.** The horizontal bar shows the application time of 5 μM HpTx2. The squares represent the normalized tail current amplitude at −10mV. Gray lines show the fits to the time courses of HpTx2 inhibition and wash-out. The best fits were derived assuming four independent binding sites. $\tau_{on} = 10.0 \pm 1.3$ s, and $\tau_{off} = 28.2 \pm 2.3$ s (Table 2). *(B)* Alignment of the S3b TMS of Kv4.1 and Kv4.3. The boundaries of S3b and the amino-terminal portion of S4 are marked below (Long et al., 2007). The amino acids critical for HpTx2 gating modification (L275 and V276) are shown in bold and underlined. Non-conserved amino acids are shaded. *(C-D)* HpTx2 does not modify gating of Kv4.1 [(L275,F276)A]. *(C)* Current traces of Kv4.1 [(L275,F276)A] in the presence of 5 μM HpTx2 (gray), performed and plotted as in Fig. 1C. *(D)* The current-voltage relationship was determined as in Fig. 1. Closed triangles connected by a black line are the controls; open triangles connected by a gray line represent normalized current after application of 5 μM HpTx2. Data are shown as mean ± S.E.M., n=6.

**Figure 3.** The S3b ‘swap’ mutants exchange phenotypes between Kv4.3 and Kv4.1 with regard to HpTx2 interaction. Panels in the top are from Kv4.1[VMTN] (square symbols; A-D), and the middle row from Kv4.3[FVPK](circles; E-F). *(A, E)* Representative current traces of Kv4.1[VMTN] and Kv4.3[FVPK], respectively, in the presence of 2 μM HpTx2 (gray), performed and plotted as in Fig. 1C. *(B-D)* Normalized $I$-$V$, $G$-$V$, and voltage-dependence of steady-state inactivation of Kv4.1 [275VMTN] in response to application of HpTx2. *(G-H)* Normalized $I$-$V$, $G$-$V$, and voltage-dependence of steady-state inactivation of Kv4.3 [275FVPK] in response to application of HpTx2. *(I)* Summary of the shifts in voltage-dependence of conductance and steady-state
inactivation (expressed as ΔV½, summarized in Table 1) of the wild type and mutant channels in response to toxin. The shaded bars represent Kv4.3, the open bars Kv4.1; the shaded crosshatched bars represent Kv4.3 [275FVPK], and the open crosshatched bars are Kv4.1 [275VMTN]. The control values for each of the S3b swap mutant channels are nearly identical to those of its wild-type parent. (J, K) Changing the S3b sequence swaps HpTx2 inhibition time courses. Representative experiments showing Kv4.1 [275VMTN] (panel J) in the presence of 2 μM HpTx2, and Kv4.3 [275FVPK] with 5 μM HpTx2 (panel K). The time courses were fit as in Fig. 2, A assuming four toxin binding sites. The time constants and Kd values are listed in Table 2. The pulse protocols and fitting algorithms are described in Materials and Methods. Panels B-D, and F-I are presented as mean values ± S.E.M, n=6.

Figure 4. Modeling schemes. (A) Scheme 1 is a Markov model for Kv4.3 or Kv4.1 in the absence of toxin, (B) Scheme 2 shows the addition of four toxin bound states for each state in Scheme 1. The parameters used to generate the model are in Table 3.

Figure 5. The Kv4 activation model reproduces both Kv4.1 activation and deactivation. (A) current traces of activation vs. time after pulses to −30 to +50 mV in 10 mV increments from the −90 mV holding potential. (B), current traces of deactivation from a +50 mV pulse to a range of voltages from −120 to −50 mV in 10 mV increments. (C-D), simulations of the experiments in A and B. (E-F) Activation and deactivation time constants for Kv4.1 (E) and Kv4.3 (F) plotted against voltage. The solid lines represent predictions derived from the Kv4 activation models. The experimental data was
collected at 16° C and the simulations were performed with the model parameters adjusted to 16° C (reduction of the rate constants by a factor 1.78 and replacement of T = 295° K by T = 289° K). (G-H) Time to peak current for Kv4.1 and Kv4.3 in the presence of HpTx2. Protocol the same as in Fig 1, A; from a holding potential of −90 mV for Kv4.1 (A; squares) and Kv4.3 (B; circles) in the presence of 2 μM HpTx2 (open symbols). The pulse protocols and fitting functions are described in Materials and Methods. Data are plotted as mean ± S.E.M., n=4-6.

**Figure 6. The Kv4 activation models reproduce HpTx2 gating modification.** (A) Time courses of interaction (represented as τ_{on} and τ_{off}), and dissociation constants for Kv4.1 (white) and Kv4.3 (gray). Open bars represent experimental data as mean ± S.E.M., n=6, calculated from Fig 2, A for Kv4.1 or from DeSimone, et al. (2009) for Kv4.3. Values predicted by our Markov model are shown in adjacent bars (checkered). (B-E) Actual and predicted normalized I-V (B-C) and G-V relationships (D-E) for Kv4.1 (B, D) and Kv4.3 (C, E) under control conditions (filled symbols) or in the presence of 2μM HpTx2 (open symbols). The data is from Fig 1, A-B, while the line is that predicted by our Markov model; black lines are under control conditions and gray lines represent the presence of toxin.

**Figure 7. The voltage dependencies of state occupancy explain the differences in HpTx2 voltage dependency in Kv4.3 and Kv4.1.** (A-B) Relative state occupancy of Kv4.1 (A) and Kv4.3 (B) at different voltages in the absence (open bars) and presence of 2 μM HpTx2 (cross-hatched bars). Positive values represent the proportion of
channels that are open (in white). Values below the origin represent channels occupying a closed state; C0-C3 are gray, and C4 is black. A bar completely below the origin represents channels that occupy only closed states, while a bar completely above the origin represents channels that are 100% open. In the presence of toxin, and at low voltages more toxin bound Kv4.1 channels open than toxin bound Kv4.3 channels because of the lower voltage dependence of the Kv4.1 C0 to C3 transitions, but as voltages increase, accumulation of toxin bound Kv4.1 in the C4 state is more prominent. (C) The influence of 2μM HpTx2 (crosshatched bars) on the relative occupancy of Kv4.1 (gray) and Kv4.3 (white) in the C4 state. The increasing prominence of the C4 state in toxin-bound Kv4.1 correlates with the lack of voltage sensitivity of HpTx2 – Kv4.1 interaction.
### Table 1: Influence of HpTx2 on $V_{1/2}$ and k values of steady-state channel properties

<table>
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<th>Channel</th>
<th>Conductance</th>
<th>Steady-State Inactivation</th>
</tr>
</thead>
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<tr>
<td></td>
<td>Control</td>
<td>+HpTx2</td>
</tr>
<tr>
<td></td>
<td>$V_{1/2}$</td>
<td>k</td>
</tr>
<tr>
<td>Kv4.1</td>
<td>-1.8 ± 0.7</td>
<td>16.4 ± 0.4</td>
</tr>
<tr>
<td>Kv4.3</td>
<td>6.1 ± 0.7</td>
<td>16.1 ± 0.2</td>
</tr>
<tr>
<td>Kv4.1 [(L275,F276)A]</td>
<td>4.4 ± 0.7</td>
<td>14.0 ± 0.6</td>
</tr>
<tr>
<td>Kv4.1 [276VMTN]</td>
<td>0.1 ± 1.0</td>
<td>16.8 ± 0.1</td>
</tr>
<tr>
<td>Kv4.3 [276FVPK]</td>
<td>6.8 ± 0.5</td>
<td>15.0 ± 0.1</td>
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<td>Kv4.1 model</td>
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<tr>
<td>Kv4.3 model</td>
<td>9.6</td>
<td>16.0</td>
</tr>
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</table>

All numbers given in mV as mean ± S.E.M., n=4-6. The [HpTx2] was 2 μM except for Kv4.1[(L275,F276)A] with which 5 μM HpTx2 was used. Kv4.3 conductance values are from DeSimone, et al. (2009). N/A: Not applicable.
Table 2: HpTx2 rate constants

<table>
<thead>
<tr>
<th>Channel</th>
<th>$\tau_{on}$ (s)</th>
<th>$\tau_{off}$ (s)</th>
<th>$k_{on}$ (M$^{-1}$·s$^{-1}$)</th>
<th>$k_{off}$ (s$^{-1}$)</th>
<th>$K_d$ (µM)</th>
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<td>10.0 ± 1.3</td>
<td>28.2 ± 2.3</td>
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<td>$K_v$4.3</td>
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<td>$K_v$4.3 [276FVPK]*</td>
<td>9.3 ± 1.6</td>
<td>22.4 ± 0.7</td>
<td>5380 ± 920</td>
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<td>$K_v$4.1 [276VMTN]</td>
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<td>0.0120</td>
<td>0.92</td>
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*$k_{on}$ calculated in the presence of 5µM HpTx2; unmarked rows calculated with 2 µM HpTx2.

$K_v$4.3 rate constants are from DeSimone, et al. (2009).
### Table 3: Model Parameters

<table>
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<th>Parameter</th>
<th>Control</th>
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<td></td>
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<td>Kv4.3*</td>
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<td>276.25 s⁻¹</td>
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<tr>
<td>a₂</td>
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<tr>
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<td>b₂</td>
<td>22.68 s⁻¹</td>
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<tr>
<td>kₒᵯ</td>
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<td>0.0286 s⁻¹</td>
</tr>
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</table>

*From Wang, et al. (2004)*

Calculation of rate constants of activation in 2mM K⁺:

\[
\alpha = f_\alpha (a_1 \exp(z_\alpha_1 e_0 VF/RT) \exp((V+10.0)/10.0) + a_2 \exp(z_\alpha_2 e_0 VF/RT))
\]

\[
\beta = f_\beta (b_1 \exp(z_\beta_1 e_0 VF/RT) \exp((V+5.0)/10.0) + b_2 \exp(z_\beta_2 e_0 VF/RT))
\]

where factors

\[
f_\alpha = 1/(1+\exp((V+10.0)/10.0))
\]

\[
f_\beta = 1/(1+\exp((V+5.0)/10.0))
\]

Net current through the channel is given by

\[
I = G_{\text{max}} P_{\theta}(V-E_K) \quad \text{where} \quad E_K = (RT/F)\ln([K^+]/[K^+]_0)
\]
Figure 1
Figure 2

A

Normalized Current

Time (s)

0 200 400 600 800

B

Kv4.1
PYYIGLEVPKDNDVSGAFVTLLRVFRVF

Kv4.3
PYYIGLVMTNEDVSGAFVTLLRVFRVF

S3b

S4

C

D

Normalized Current

Voltage (mV)

-80 -60 -40 -20 0 20 40

0.0 0.2 0.4 0.6 0.8 1.0
Figure 4

A

\[ \begin{align*}
C_0 & \rightleftharpoons C_1 \rightleftharpoons C_2 \rightleftharpoons C_3 \rightleftharpoons C_4 \rightleftharpoons O \\
\beta & \quad 2\beta \quad 3\beta \quad 4\beta \quad k_{oc}
\end{align*} \]

Scheme 1

B

Scheme 2
Figure 5
Figure 6

A

![Graph showing \( \tau_{\text{on}}, \tau_{\text{off}}, \text{and} \ K_d \)]

B

![Graph showing \( I/I_{\text{max}} \) vs. voltage (mV)]

C

![Graph showing \( I/I_{\text{max}} \) vs. voltage (mV)]

D

![Graph showing \( G/G_{\text{max}} \) vs. voltage (mV)]

E

![Graph showing \( G/G_{\text{max}} \) vs. voltage (mV)]
Figure 7

A

B

C

Voltage (mV)

State occupancy

100% open

100% closed

Voltage (mV)

% C4

Voltage (mV)